# ACHARYA INSTITUTE OF TECHNOLOGY Bangalore - 560090

# CBCS Scheme

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# Third Semester B.E. Degree Examination, Dec.2016/Jan.2017 Engineering Mathematics – III

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing one full question from each module.

## Module-1

1 a. Expand  $f(x) = x - x^2$  as a Fourier series in the interval  $(-\pi, \pi)$ . (08 Marks)

b. Obtain the half-range cosine series for the function f(x) = x (l - x) in the interval  $0 \le x \le l$ .

(08 Marks)

#### OR

2 a. Obtain the Fourier series of  $f(x) = \frac{\pi - x}{2}$  in  $0 < x < 2\pi$ . Hence deduce that

$$\frac{\pi}{4} = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots$$
 (06 Marks)

b. Find the half-range sine series for the function

$$f(x) = \begin{cases} \frac{1}{4} - x & \text{in } 0 < x < 1/2 \\ x - \frac{3}{4} & \text{in } 1/2 < x < 1 \end{cases}$$
 (05 Marks)

c. Compute the constant term and the coefficient of the 1<sup>st</sup> sine and cosine terms in the Fourier series of y as given in the following table:

(05 Marks)

## Module-2

3 a. If  $f(x) = \begin{cases} 1 - x^2; & |x| < 1 \\ 0; & |x| \ge 1 \end{cases}$ . Find the Fourier transform of f(x) and hence find the value of

$$\int_{0}^{\infty} \frac{x \cos x - \sin x}{x^{3}} dx . \tag{06 Marks}$$

b. Find the Fourier sine and cosine transform of

$$f(x) = \begin{cases} x, & 0 < x < 2 \\ 0, & \text{elsewhere} \end{cases}$$
 (05 Marks)

c. Solve using Z-transform  $y_{n+2} - 4y_n = 0$  given that  $y_0 = 0$ ,  $y_1 = 2$ . (05 Marks)

#### OR

4 a. Obtain the inverse Fourier sine transform of  $F_s(\alpha) = \frac{e^{-a\alpha}}{\alpha}$ , a > 0. (06 Marks)

b. Find the Z-transform of 
$$2n + \sin\left(\frac{n\pi}{4}\right) + 1$$
. (05 Marks)

c. If 
$$U(z) = \frac{z}{z^2 + 7z + 10}$$
, find the inverse Z-transform. (05 Marks)

### Module-3

5 a. Obtain the coefficient of correlation for the following data:

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x:	10	14	18	22	26	30
y:	18	12	24	6	30	36

(06 Marks)

b. By the method of least square find the straight line that best fits the following data:

x:	1	2	3	4	5
y:	14	27	40	55	68

(05 Marks)

c. Use Newton-Raphson method to find a root of the equation tanx - x = 0 near x = 4.5. Carry out two iterations. (05 Marks)

### OR

6 a. Find the regression line of y on x for the following data:

	x:	1	3	4	6	8	9	11	14
	y:	1	2	4	4	5	7	8	9

Estimate the value of y when x = 10.

(06 Marks)

b. Fit a second degree parabola to the following data:

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X	0	1	2	3	4
У	1	1.8	1.3	2.5	6.3

(05 Marks)

c. Solve  $xe^x - 2 = 0$  using Regula – Falsi method.

(05 Marks)

## Module-4

7 a. From the data given in the following table. Find the number of students who obtained less than 70 marks.

Marks:	0-19	20-39	40-59	60-79	80-99
Number of students:	41	62	65	50	17

(06 Marks)

b. Find the equation of the polynomial which passes through the points (4, -43), (7, 83), (9, 327) and (12, 1053). Using Newton's divided difference interpolation. (05 Marks)

c. Compute the value of  $\int_{0.2}^{1.4} (\sin x - \log x + e^x) dx$  using Simpson's  $\frac{3}{8}^{th}$  rule taking six parts.

(05 Marks)

#### OR

8 a. Using Newton's backward interpolation formula find the interpolating polynomial for the function given by the following table:

x:	10	11	12	13
f(x):	22	24	28	34

Hence fine f(12.5).

(06 Marks)

b. The following table gives the premium payable at ages in years completed. Interpolate the premium payable at age 35 completed. Using Lagrange's formula.

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	Age completed:	25	30	40	60	
	Premium in Rs.:	50	55	70	95	

(05 Marks)

c. Evaluate  $\int_{4}^{5.2} \log_e x \, dx$  taking 6 equal strips by applying Waddles rule. (05 Marks)

# 15MAT31

- a. Verify Green's theorem for  $\oint (xy + y^2)dx + x^2dy$  where c is the closed curve of the region bounded by y = x and y = xz. (06 Marks)
  - b. Verify Stoke's theorem for  $\vec{F} = (x^2 + y^2)i 2xyj$  taken round the rectangle bounded by the lines  $x = \pm a$ , y = 0 and y = b. (05 Marks)
  - c. A heavy cable hangs freely under gravity between two fixed points. Show that the shape of the cable is a catenary. (05 Marks)

- Use divergence theorem to evaluate  $\iint \vec{F} \hat{n}$  ds over the entire surface of the region above XoY plane bounded by the cone  $z^2=x^2+y^2$ , the plane z=4 where  $\vec{F}=4xz^1\hat{i}+xyz^2\hat{j}+3z\hat{k}$ .
  - Find the extremal of the functional  $\int_{x_1}^{x_2} [(y^1)^2 y^2 + 2y \sec x] dx$ . (05 Marks)
  - Prove that the shortest distance between two points in a plane is along the straight line joining them. (05 Marks)