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10AE64

**Sixth Semester B.E. Degree Examination, June/July 2019**  
**Finite Element Analysis**

Time: 3 hrs.

Max. Marks: 100

*Note: Answer any FIVE full questions, selecting at least TWO questions from each part.*

**PART - A**

- 1 a. Explain with a sketch, plane stress and plane strain for two dimensions with notations. (08 Marks)
- b. Using Rayleigh Ritz method, derive an expression for the displacement of a Cantilever beam subjected to uniformly distributed load  $P_0$  over entire length as shown in Fig. Q1 (b). (12 Marks)

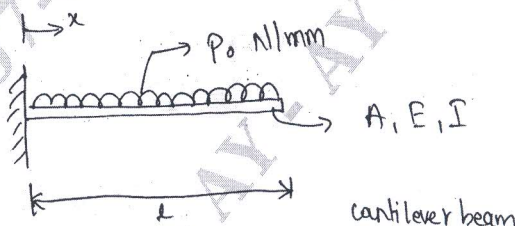


Fig. Q1 (b)

where  $E$  – Young's modulus,  $I$  – moment of inertia and  $A$  is area of cross section.

- 2 a. Differentiate between global local and natural co-ordinate system. (06 Marks)
- b. Explain the convergence criteria with suitable examples. (04 Marks)
- c. Derive the shape function for a two noded beam element. (10 Marks)
- 3 a. What do you mean by boundary conditions in FEM? Explain in brief. (04 Marks)
- b. Consider the four-bar truss as shown in Fig. Q3 (b). It is given that  $E = 2 \times 10^5 \text{ N/mm}^2$  and  $A_e = 100 \text{ mm}^2$  for all elements:
  - (i) Determine the element stiffness matrix for each element.
  - (ii) Assemble the elemental stiffness matrix  $K$  for entire element.
  - (iii) Using elimination approach for the nodal displacement.
  - (iv) Calculate stresses in each element.
  - (v) Calculate the reaction forces.

(16 Marks)

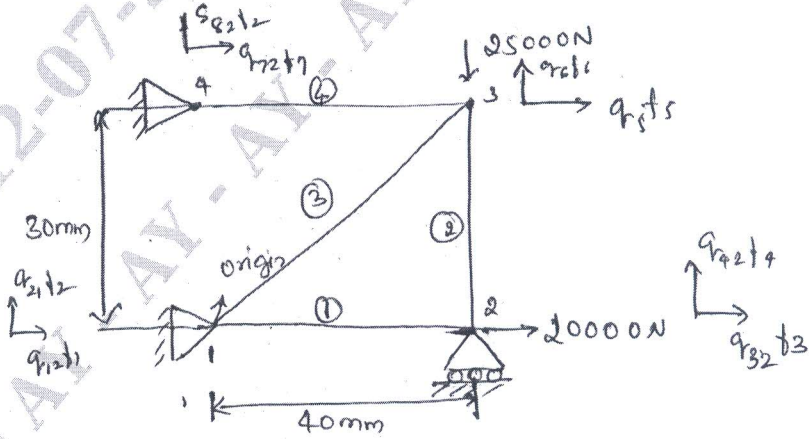


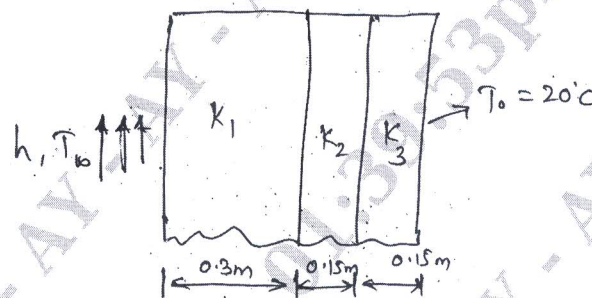
Fig. Q3 (b)  
1 of 2

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
 2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.

- 4 a. Derive the shape functions for a rectangular element with usefull notations. Use natural co-ordinate system. (10 Marks)  
 b. Derive the shape function for a Linear Strain Triangular (LST) element. Use natural co-ordinate system. (10 Marks)

**PART - B**

- 5 a. Explain the method of finding the shape functions for hexahedral element. (10 Marks)  
 b. Discuss about serendipity family and Langrange family. (08 Marks)  
 c. Define a shape function. (02 Marks)
- 6 a. Explain the concept of isoparametric, subparametric and super parametric elements and their uses. (10 Marks)  
 b. Explain pre and post processing in FEA and List out various applications of FEA in engineering. (10 Marks)
- 7 a. Explain the concept of axysymmetric element . (04 Marks)  
 b. Using the shape functions discuss the finite element modeling of triangular element of axisymmetric element. (16 Marks)
- 8 a. A composite wall consists of three materials as shown in Fig. Q8 (a). The outer temperature is  $T_0 = 20^\circ\text{C}$ . Convection heat transfer takes place on the inner surface of the wall with  $T_\infty = 800^\circ\text{C}$  and  $h = 25 \text{ W/m}^2\text{C}$ . Determine the temperature distribution in the wall. (16 Marks)



$$\begin{aligned} K_1 &= 20 \text{ W/m}^\circ\text{C} \\ K_2 &= 30 \text{ W/m}^\circ\text{C} \\ K_3 &= 50 \text{ W/m}^\circ\text{C} \\ h &= 25 \text{ W/m}^2\text{C} \\ T_\infty &= 800^\circ\text{C} \end{aligned}$$

Fig. Q8 (a)

- b. Write four properties of shape functions. (04 Marks)

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