

Fourth Semester B.E. Degree Examination, June/July 2019

Signals and Systems

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, selecting at least TWO full questions from each part.

PART - A

- 1 a. Define signal and system with examples. (06 Marks)

- b. Prove that

i) $\int_{-a}^a x(t)dt = \alpha \int_0^a x(t)dt$ If $x(t)$ is even ii) $\int_{-a}^a x(t)dt = 0$ If $x(t)$ is odd. (06 Marks)

- c. For the following system, determine whether the system is a) Linear b) Time invariant
c) Memory less d) Causal.

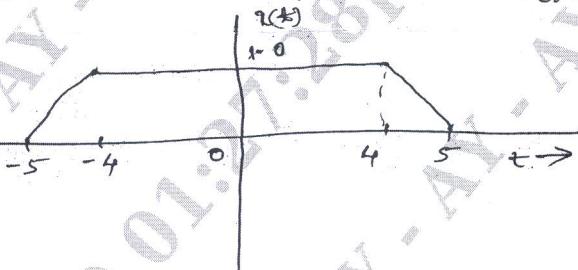
i) $T[x(n)] = g(n)x(n)$ ii) $T[x(t)] = e^{xt}$ (08 Marks)

- 2 a. The trapezoidal signal as shown in Fig.Q.2(a) applied to differentiator defined by

$$y(t) = \frac{d}{dt}x(t)$$

- i) Find the resulting output of differentiator ii) Find the total energy of $y(t)$. (06 Marks)

Fig.Q.2(a)



- b. Find the discrete-time convolution sum of $y(n) = \beta^n u(n) * \alpha^n u(n)$ $|\alpha| < 1 : |\beta| < 1$. (06 Marks)

- c. Consider a continuous-time LTI system with unit impulse response $h(t) = u(t)$ and input $x(t) = e^{-at} u(t)$ $|a| > 0$. Find the output $y(t)$. (08 Marks)

- 3 a. Prove that

i) $x(n) * h(n) = h(n) * x(n)$
ii) $x(n) * [h_1(n) + h_2(n)] = x(n) * h_1(n) + x(n) * h_2(n)$ (08 Marks)

- b. Find the output of the system given by the differential equation:

$$\frac{d^2y(t)}{dt^2} + 5\frac{dy(t)}{dt} + 4y(t) = \frac{dx(t)}{dt} \quad \text{with } y(0) = 0 \quad \left. \frac{dy(t)}{dt} \right|_{t=0} = 1 \quad \text{and } x(t) = e^{-2t} u(t).$$

(06 Marks)

- c. Draw the direct form I and direct form II implementation of the following system shown below:

i) $\frac{d^3y(t)}{dt^3} + 2\frac{dy(t)}{dt} + 3y(t) = x(t) + 3\frac{dx(t)}{dt}$

ii) $y(n) - \frac{1}{4}y(n-1) + \frac{1}{8}y(n-2) = x(n) + \frac{1}{2}x(n-2)$ (06 Marks)

- 4 a. Determine the DTFS of the signal

i) $x(n) = \cos\left(\frac{\pi}{3}n\right)$

ii) $x(n) = \sum_{M=-\infty}^{\infty} \delta(n - 4m)$

(08 Marks)

- b. Determine the FS representation for the signal

i) $x(t) = \cos 4t + \sin 8t$ ii) $x(t) = e^{-t}$
 $-1 < t < 1$
 $T = 2$

(08 Marks)

- c. Prove the following properties:

i) If $x(t) \xleftarrow{FS, w_0} x(k)$ then $y(t) = x(t - t_0) \xleftarrow{FS, w_0} y(k) = e^{-jkw_0 t_0} x(k)$

ii) If $x(t) \xleftarrow{FS, w_0} x(k)$ then $y(t) = e^{jk_0 w_0 t} x(t) \xleftarrow{FS, w_0} y(k) = x(k - k_0)$. (04 Marks)

PART - B

- 5 a. Compute DTFT of the following signals:

i) $x(n) = 2^n u(-n)$ ii) $x(n) = a^{|n|}$ $|a| < 1$

(08 Marks)

- b. Find the Fourier transform of $x(t) = e^{-a|t|}$ $a > 0$. Draw its spectrum.

(06 Marks)

- c. Find the inverse Fourier transform:

i) $x(jw) = \frac{5jw + 12}{(jw)^2 + 5jw + 6}$

ii) $x(jw) = \frac{jw}{(2 + jw)^2}$

(06 Marks)

- 6 a. Find the relationship between: i) FT and FS ii) DTFT and DTFS. (08 Marks)

- b. Specify the Nyquist rate for each signals :

i) $x_1(t) = \text{sinc}(200t)$ ii) $x_2(t) = \text{sinc}^2(200t)$

(06 Marks)

- c. Find the frequency response and impulse response of the following system:

$$\frac{d^2y(t)}{dt^2} + 5 \frac{dy(t)}{dt} + 6y(t) = - \frac{dx(t)}{dt}$$

(06 Marks)

- 7 a. Determine the Z-transform, ROC, pole zero location of the following system:

i) $x(n) = \alpha^n u(n)$

ii) $x(n) = -\alpha^n u(-n-1)$

iii) $x(n) = a^n \cos(\Omega_o n) u(n)$ for $\Omega_o = 2\pi$.

(09 Marks)

- b. Explain the properties of ROC.

(06 Marks)

- c. Prove that

i) $x(n - n_0) \xleftarrow{z} z^{-n_0} x(z)$

ii) $a^n x(n) \xleftarrow{z} x\left(\frac{z}{a}\right)$

(05 Marks)

- 8 a. Determine whether the system described below is causal and stable

$$H(z) = \frac{2z+1}{z^2 + z - 5/16}.$$

(06 Marks)

- b. Consider a system described by the difference equation.

$$y(n) - 2y(n-1) + 2y(n-2) = x(n) + \frac{1}{2}x(n-1)$$

Find: i) $H(z)$ ii) $h(n)$ iii) Stability.

(08 Marks)

- c. What is unilateral Z-transform and prove its time shifting property.

(06 Marks)

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