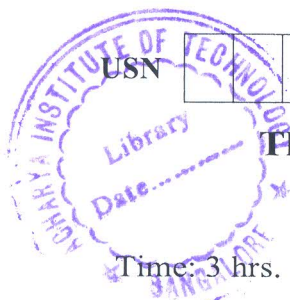


CBCS SCHEME

17MATDIP31



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Third Semester B.E. Degree Examination, June/July 2019 Additional Mathematics – I

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Find the sine of the angle between $\vec{a} = 2\hat{i} - 2\hat{j} + \hat{k}$ and $\vec{b} = \hat{i} - 2\hat{j} + 2\hat{k}$. (08 Marks)
- b. Express the complex number $\frac{(1+i)(1+3i)}{1+5i}$ in the form $a + ib$. (06 Marks)
- c. Find the modulus and amplitude of $\frac{(1+i)^2}{3+i}$. (06 Marks)

OR

- 2 a. Show that $(1 + \cos \theta + i \sin \theta)^n + (1 + \cos \theta - i \sin \theta)^n = 2^{n+1} \cdot \cos^n \left(\frac{\theta}{2} \right) \cdot \cos \left(\frac{n\theta}{2} \right)$. (08 Marks)
- b. If $\vec{a} = 2\hat{i} + 3\hat{j} - 4\hat{k}$ and $\vec{b} = 8\hat{i} - 4\hat{j} + \hat{k}$, then prove that \vec{a} is perpendicular to \vec{b} . Also find $|\vec{a} \times \vec{b}|$. (06 Marks)
- c. Determine λ such that $\vec{a} = \hat{i} + \hat{j} + \hat{k}$, $\vec{b} = 2\hat{i} - 4\hat{k}$ and $\vec{c} = \hat{i} + \lambda\hat{j} + 3\hat{k}$ are coplanar. (06 Marks)

Module-2

- 3 a. If $y = \cos(m \log x)$ then prove that $x^2 y_{n+2} + (2n+1)xy_{n+1} + (m^2 + n^2)y_n = 0$. (08 Marks)
- b. Find the angle of intersection of the curves $r^2 \sin 2\theta = a^2$ and $r^2 \cos 2\theta = b^2$. (06 Marks)
- c. Find the pedal equation of the curve $r = a(1 + \sin \theta)$. (06 Marks)

OR

- 4 a. Obtain the Maclaurin's series expansion of $\log \sec x$ up to the terms containing x^6 . (08 Marks)
- b. If $u = \operatorname{cosec}^{-1} \left(\frac{x^{\frac{1}{2}} + y^{\frac{1}{2}}}{x^{\frac{1}{3}} + y^{\frac{1}{3}}} \right)$, prove that $xu_x + yu_y = -\frac{1}{6} \tan u$. (06 Marks)
- c. Find $\frac{\partial(u, v, w)}{\partial(x, y, z)}$ where $u = x + y + z$, $v = y + z$, $w = z$. (06 Marks)

Module-3

- 5 a. Obtain a reduction formula for $\int_0^{\pi/2} \sin^n x dx$, ($n > 0$). (08 Marks)
- b. Evaluate $\int_0^{2a} x^2 \sqrt{2ax - x^2} dx$. (06 Marks)
- c. Evaluate $\int_0^1 \int_x^{\sqrt{x}} xy dy dx$ (06 Marks)

OR

- 6 a. Evaluate $\int_0^a \int_0^x \int_0^{x+y} e^{x+y+z} dz dy dx$. (08 Marks)
- b. Evaluate $\int_0^{\infty} \frac{x^6}{(1+x^2)^{9/2}} dx$. (06 Marks)
- c. Evaluate $\iint_A xy dx dy$ where A is the area bounded by the circle $x^2 + y^2 = a^2$ in the first quadrant. (06 Marks)

Module-4

- 7 a. A particle moves along the curve $\vec{r} = \cos 2t \hat{i} + \sin 2t \hat{j} + t \hat{k}$. Find the components of velocity and acceleration at $t = \frac{\pi}{8}$ along $\sqrt{2} \hat{i} + \sqrt{2} \hat{j} + \hat{k}$. (08 Marks)
- b. Find divergence and curl of the vector $\vec{F} = (xyz + y^2z) \hat{i} + (3x^2 + y^2z) \hat{j} + (xz^2 - y^2z) \hat{k}$. (06 Marks)
- c. Find the directional derivative of $\phi = x^2yz^3$ at (1, 1, 1) in the direction of $\hat{i} + \hat{j} + 2\hat{k}$. (06 Marks)

OR

- 8 a. Find the angle between the tangents to the curve $x = t^2, y = t^3, z = t^4$ at $t = 2$ and $t = 3$. (08 Marks)
- b. Find $\text{curl}(\text{curl } \vec{A})$ where $\vec{A} = xy \hat{i} + y^2z \hat{j} + z^2y \hat{k}$. (06 Marks)
- c. Find the constants a, b, c such that the vector field $(\sin y + az) \hat{i} + (bx \cos y + z) \hat{j} + (x + cy) \hat{k}$ is irrotational. (06 Marks)

Module-5

- 9 a. Solve $\frac{dy}{dx} = \frac{y}{x} + \sin\left(\frac{y}{x}\right)$. (08 Marks)
- b. Solve $\frac{dy}{dx} + y \cot x = \sin x$. (06 Marks)
- c. Solve $\frac{dy}{dx} + \frac{y}{x} = y^2x$. (06 Marks)

OR

- 10 a. Solve $x^2 y dx - (x^3 + y^3) dy = 0$. (08 Marks)
- b. Solve $x^2 \frac{dy}{dx} = 3x^2 - 2xy + 1$. (06 Marks)
- c. Solve $\left[y \left(1 + \frac{1}{x} \right) + \cos y \right] dx + [x + \log x - x \sin y] dy = 0$. (06 Marks)
