

15EE63

Sixth Semester B.E. Degree Examination, Dec.2019/Jan.2020 **Digital Signal Processing**

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- a. Find 4 point DFT of $x(n) = \{1, -2, 3, 4\}$ and plot magnitude and phase response. (06 Marks) 1
 - If $x_1(n) = \{2, 3, 1, 1\}$ and $x_2(n) = \{1, 3, 5, 3\}$, find $x_3(n) = x_1(n)$ 4 $x_2(n)$ use matrix method (06 Marks)
 - Prove the time reversal property of DFT.

(04 Marks)

OR

- a. Perform circular convolution of $x_1(n) = \{2, 1, 2, 1\}$ and $x_2(n) = \{1, 2, 3, 4\}$ using circular shift method.
 - b. Find linear convolution using DFT for the given sequence $x(n) = \{1, 2, 3\}$ $h(n) = \{1, 2, 2, 1\}.$ (06 Marks)
 - Find the IDFT of the given sequence $x(k) = \{3, 2 + j, 1, 2 j\}$.

(05 Marks)

Module-2

- 3 Find the 8-point DFT of sequence $x(n) = \{1, 1, 1, 1, 0, 0, 0, 0\}$ using DIT FFT radix 2 algorithm. Draw signal graph.
 - b. Develop a Decimation in Frequency FFT algorithm for N = 8. Draw signal flow graph. (08 Marks)

- Develop a decimation in time algorithm FFT of N = 8 draw signal flow graph. (08 Marks)
 - Calculate 8-point DFT of sequence $x(n) = \{1, -1, -1, -1, 1, 1, 1, -1\}$, using DIF FFT radix -2 algorithm. (08 Marks)

Module-3

Design an analog Chebyshev with following specification. 5

Passband : 1db for $0 \le \Omega \le 10$ rad/sec

Stopband attenuation : -60 db for $\Omega \ge 50$ rad/sec.

(10 Marks)

The system function of an analog filter is given as $H_a(s) = \frac{1}{(s+1)(s+2)}$. Obtain H(z) using impulse invariant method take sampling frequency as 5 samples/sec.

(06 Marks)

- Design a low pass Butterworth filter using bilinear transformation method to meet the following specification take T = 2sec

Passband ripple $\leq 1.25 dB$

Passband edge = 200 Hz

Stopband attenuation $\geq 15 dB$

Stopband edge = 400Hz

Sampling frequency = 2KHz

(10 Marks)

Prove the following transformation relation for impulse invariant transform.

$$\frac{s+a}{(s+a)^2+b^2} = \frac{1-e^{aT}(\cos bT)z^{-1}}{1-2e^{-aT}(\cos bT)z^{-1}+e^{-2aT}z^{-2}}$$
(06 Marks)

Module-4

- Compare bilinear transformation with impulse invariance transformation. (04 Marks)
 - Write a note on frequency warping.

(06 Marks)

- c. Determine Direct form I and II for 2nd order filter given by
 - $y(n) = 2b \cos w_0 y(n-1) b^2 y(n-2) + x(n) b \cos w_0 x(n-1)$

(06 Marks)

Obtain the Cascade form realization for given system.

$$H(z) = \frac{(z-1)(z-2)(z+1)z}{\left(z - \frac{1}{2} - \frac{1}{2}j\right)\left(z - \frac{1}{2} + \frac{1}{2}j\right)\left(z - \frac{1}{4}j\right)\left(z + \frac{1}{4}j\right)}$$
(08 Marks)

b. Design a second order lowpass digital Butterworth filter with cutoff frequency 1KHz and sampling frequency of 10⁴ samples/sec by linear transformation. (08 Marks)

Module-5
Given the FIR filter with following deference equation 9

$$y(n) = x(n) + \frac{2 \cdot x}{5}(n-1) + \frac{3}{4}x(n-2) + \frac{1}{3}x(n-3)$$
. Draw direct Form – I and lattice structure.

b. Using frequency sampling method, design a band pass filter with following specification determine the filter coefficient for N = 7, sampling frequency F = 8000Hz, cutoff frequency $f_{c_1} = 1000 \text{Hz}, f_{c_2} = 3000 \text{Hz}$

Realise the following system function in cascade form

$$H(z) = 1 + \frac{3}{4}z^{-1} + \frac{17}{8}z^{-2} + \frac{3}{4}z^{-3} + z^{-4}$$
 in direct form I and cascade form. (08 Marks)

b. Design the symmetric FIR lowpass filter whose desired frequency response is given as
$$H_{d}(\omega) = \begin{cases} e^{-j\omega z}, & \text{for } |\omega| \leq \omega_{c} \\ 0, & \text{otherwise} \end{cases}$$

The length of filter should be 7 and $\omega_c = 1$ rad/sample use rectangular window. (08 Marks)