

17EE54

Fifth Semester B.E. Degree Examination, Jan./Feb. 2021 Signals and Systems

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

a. Explain Classification of Signals.
b. A signal x(t) = u(t), unit step function. Sketch and label each of the following signals:

i) x(t-2) ii) x(-t) iii) x(t+2) iv) s(t/2). (08 Marks)

c. Determine whether the following signals are periodic, if periodic determine the fundamental period:

i) $x(t) = \cos 2t + \sin 3t$ ii) $x(n) = \cos (1/5 \pi n) \sin (\frac{1}{3} \pi n)$. (06 Marks)

OR

2 a. What are different elementary signals? Explain them, with neat sketch. (04 Marks)

b. For the system given below, determine whether or not the system is linear causal, time invariant, BIBO stable: i) $y(t) = e^{x(t)}$ ii) y(n) = x(n) u(n). (10 Marks)

c. Find even and odd part of following signal:

i) $x(t) = \cos(t) + \sin(t) + \sin(t) \cos(t)$ ii) x(n) = u(n). (06 Marks)

Module-2

a. Consider a LTI system with unit impulse response $h(t) = e^{-t} u(t)$. If the input to the system is $x(t) = e^{-3t} [u(t) - u(t-2)]$. Find the output y(t) of the system. (10 Marks)

b. Evaluate the discrete time Convolution sum for h[n] = u[n] and $x[n] \cdot (\frac{1}{2})^n u[n-2]$.

(06 Marks)

c. Find the step response for the CTI system represented by the impulse response $h(n) = (\frac{1}{2})^n u(n)$. (04 Marks)

OR

a. A discrete LTI system is characterized by the following difference equation. y(n) - y(n-1) - 2y(n-2) = x(n) with x(n) = 6u(n) and initial conditions y(-1) = -1, y(-2) = 4. Find the zero input response, zero state response and total response. (10 Marks)

b. Draw the direct Form I and II realization for the following system:

i)
$$y(n) - \frac{1}{2}y(n-1) + \frac{1}{4}y(n-2) = x(n) + 2x(n-1).$$

ii) $2\frac{d^3y}{dt^3} + \frac{dy(t)}{dt} + 3y(t) = x(t).$ (10 Marks)

Module-3

5 a. State and prove following properties in continuous Time Fourier Transform:

i) Time shift ii) Frequency shift iii) Convolution. (10 Marks)

b. Find Fourier transform of following signals:

i) $x(t) = e^{at} u(-t)$ ii) x(t) = 1 iii) $x(t) = \cos w_0 t$. (10 Marks)

OR

a. Using Partial fraction expansion, determine the Inverse Fourier transform of

i) $X(w) = \frac{5jw + 12}{(jw)^2 + 5jw + 6}$ ii) $X(w) = \frac{-jw}{(jw)^2 + 3jw + 2}$.

(10 Marks)

b. A system produces output of $y(t) = e^{-2t} u(t) + e^{-3t} u(t)$ for an input $x(t) = e^{-t} u(t)$ Determine the Impulse response and Frequency response of the system. (10 Marks)

Module-4

a. State and prove the following properties in DTFT

i) Parseval's theorem

ii) Differentiation in frequency domain.

(10 Marks)

b. Find DTFT of the following signal:

i)
$$x(n) = \left(\frac{1}{2}\right)^n u(n-2)$$
 ii) $x(n) = u(n)$.

(10 Marks)

a. Find Inverse DTFT of

 $X(e^{i\Omega}) = \frac{6}{e^{-j2\Omega} - 5e^{-i\Omega} + 6} \,. \label{eq:X}$

(06 Marks)

- Determine the difference equation description for the system with following impulse response $h(n) = \delta(n) + 2(\frac{1}{2})^n u(n) + (-\frac{1}{2}) u(n)$. (07 Marks)
- c. Obtain the frequency response and the impulse response of the system described by the difference equation: $y(n) + \frac{1}{2}y(n-1) = x(n) - 2x(n-1)$. (07 Marks)

What is Region of Convergence? List any five properties of RoC.

(07 Marks)

- Determine Z transform of the following signals:

 - i) $x(n) = n a^n u(n)$ ii) $x(n) = (0.2)^n \{u(n) u(n-u)\}.$

(08 Marks)

State and prove Initial value theorem of Z - transforms.

(05 Marks)

a. Using Partial Fraction expansion method, find time domain signal.

 $X(z) = \frac{z^3 - 3z}{z^2 + \frac{3}{2}z - 1}$; RoC: $\frac{1}{2} < |z| < 2$,

(06 Marks)

- b. Solve the following difference equation y(n) + 3y(n-1) = x(n), with x(n) = u(n) and Initial condition y(-1) = 1.
- c. The output of a discrete time LIT system is found to be $y(n) = 2(\frac{1}{3})$ u(n). When input is x(n) = u(n). Find Impulse response h(n) of the system. (06 Marks)