

CBCS SCHEME

USN

Librarian
Learning Resource Centre
Acharya Institute & Technology

18AE56

Fifth Semester B.E. Degree Examination, Feb./Mar. 2022

Theory of Vibrations

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Add the following harmonics analytically and check the solution graphically:
 $x_1 = 3\sin(\omega t + 30^\circ)$
 $x_2 = 4\cos(\omega t + 10^\circ)$ (10 Marks)
- b. Explain the phenomenon of the beats. (10 Marks)

OR

- 2 a. Represent the periodic motion given in Fig.Q.2(a) by Harmonic series. (12 Marks)

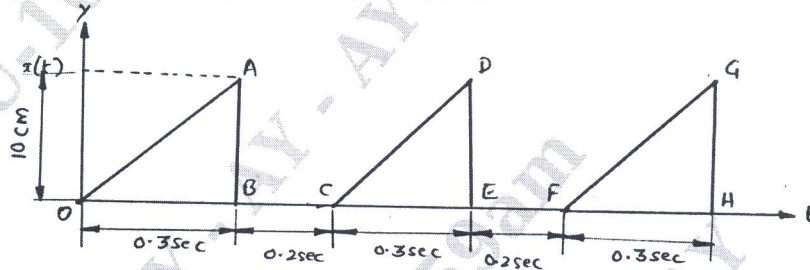


Fig.Q.2(a)

- b. Explain the types of vibration. (08 Marks)

Module-2

- 3 a. Determine the natural frequency of a spring mass system where the mass of the spring is also to be taken into account. (10 Marks)
- b. The solution to the differential equation for single degree freedom motion is given by $x = X\cos(100t + \phi)$ with initial condition $\dot{x}_{(0)} = 1250\text{mm/sec}$ and $x_{(0)} = 0.25\text{mm}$. Find the values of X and ϕ and express the given equation in the form $x = A\sin\omega_n t + B\cos\omega_n t$. (10 Marks)

OR

- 4 a. Define logarithm decrement and prove that the logarithmic decrement $\delta = \frac{1}{n} \ln \frac{x_0}{x_n}$, where x_0 is the initial and x_n is the amplitude after 'n' cycles. (10 Marks)
- b. A mass of 7.5kg hangs from a spring and makes damped oscillations. The time for 60 oscillations is 35secs and the ratio of first to seventh displacement is 2.5. Find the following:
i) Stiffness of spring
ii) Damping resistance
iii) Critical damping resistance
iv) Damping factor. (10 Marks)

Module-3

- 5 a. What is magnification factor? Derive an expression for the same and discuss its variation with frequency ratio. (10 Marks)
- b. A machine of total mass 68kg mounted on springs of stiffness 11,000 N/cm. With an assumed damping factor of 0.2. A piston within the machine has a mass of 2kg has a reciprocating motion with stroke 7.5cm and a speed of 3000rpm. Assuming the motion of piston to be S.H.M. Determine:
- Amplitude of motion.
 - Phase angle with respect to exciting force.
 - Transmissibility and force transmitted to ground.
 - Phase angle of transmitted force with respect to exciting force. (10 Marks)

OR

- 6 a. Derive an expression for critical speed of whirling of shafts without air damping. (10 Marks)
- b. A vibration pickup has a natural frequency of 7.5Hz and a damping factor of 0.5. Determine the lowest frequency beyond which the amplitude can be measured within
- 1% error
 - 2% error. (10 Marks)

Module-4

- 7 a. Fig.Q.7(a) shows a system subjected to vibration. Find an expression for the natural frequency. Locate the mode and draw mode shapes. (12 Marks)

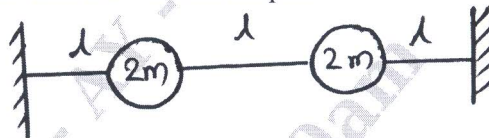


Fig.Q.7(a)

- b. Explain the following:
- Principal modes and normal modes of vibration
 - Coordinate coupling. (08 Marks)

OR

- 8 a. For the rotor system shown in Fig.Q.8(a), find the natural frequencies and mode shapes. (10 Marks)

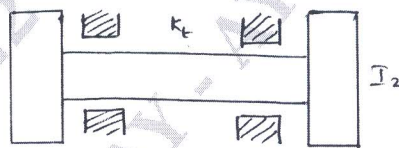


Fig.Q.8(a)

- b. For the system shown in Fig.Q.8(b), obtain the equations of motion. Also obtain the condition for system not to have elastic coupling. (10 Marks)

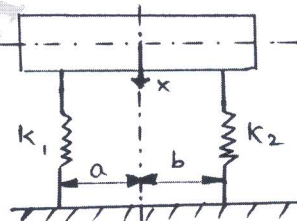


Fig.Q.8(b)

Module-5

- 9 a. State and prove Maxwell's reciprocal theorem. (08 Marks)
 b. For the system shown in Fig.Q.9(b), find the lowest natural frequency by Stodola's method.

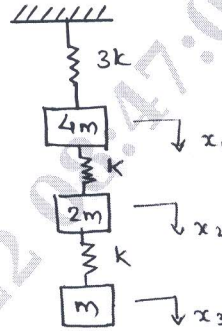


Fig.Q.9(b)

(12 Marks)

OR

- 10 Find all the natural frequencies of the four degree of freedom system shown in Fig.Q.10 by using Holzer's method.

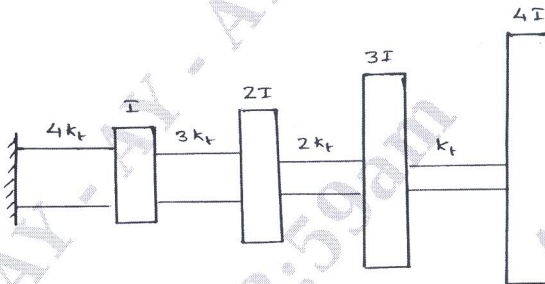


Fig.Q.10

(20 Marks)
