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## Chromatic number of Antipodal Graph

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### **Abstract**

Chromatic number of a graph is the minimum number of colors with which a graph can be colored properly. In this paper we are finding the chromatic number of Antipodal graph, also we discussed the chromatic number of different properties of Antipodal graph.

**Keywords:** *Chromatic number, Antipodal graph, complete graph, diameter.*

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### **I. INTRODUCTION:**

Singleton (1968) introduced the concept of the Antipodal graph of a graph  $G$ , denoted **Antipodal graph**

by  $A(G)$ , is the graph on the same vertices as of  $G$ , two vertices being adjacent if the distance between them is equal to the diameter of  $G$ .

### **Chromatic number of Antipodal graph**

By the motivation of existing definition of Chromatic number of a graph and Antipodal graph we can find the Chromatic number of Antipodal graph. We consider only finite undirected graphs  $G = (V, E)$  without loops and multiple edges and follow Harary [4] for notation and terminology.

### **II. RESULTS AND DISCUSSION:**

**Proposition 1. (Aravamudhan and Rajendran [1])** For a graph  $G = (V, E)$ ,  $G = A(G)$  if, and only if  $G$  is complete.

From the above result we have the following

**Proposition 2.** For a complete graph  $G = (V, E)$ ,  $\chi(G) = \chi(A(G))$

**Proof.** Since  $G$  is a complete graph and  $n$  is the number of vertices of  $G$ ,  $\chi(G) = n$  and by Proposition 1,  $G = A(G)$  hence  $\chi(G) = \chi(A(G)) = n$

For any positive integer  $k$ , the  $k^{\text{th}}$  iterated antipodal graph  $A(G)$  is defined as follows:

$$A^0(G) = A(G), \quad A^k(G) = A(A^{k-1}(G))$$

**Corollary 3.** For any graph  $G$ , and any positive integer  $k$ ,  $\chi(A^k(G)) = \chi(A(G))$

**Proposition 4. (Aravamudhan and Rajendran [1])** For a graph  $G = (V, E)$ ,  $\bar{G} = A(G)$  if, and only if, i).  $G$  is of diameter 2 or ii).  $G$  is disconnected and the components of  $G$  are complete graphs. In view of the above, we have the following result:

**Proposition 5.** For a graph  $G = (V,E)$ ,  $\chi(A(G)) = \chi(\bar{G})$  if, and only if,  
i).  $G$  is of diameter 2 or ii).  $G$  is disconnected and the components of  $G$  are complete graphs.

**Proof.** Suppose that ,  $\chi(A(G)) = \chi(\bar{G})$  then clearly we have  $A(G) = \bar{G}$  and hence  $G$  satisfies the conditions of Proposition 4.  
Conversely,  $G$  satisfies the conditions of Proposition 4 then  $\bar{G} = A(G)$ , obviously,  
 $\chi(A(G)) = \chi(\bar{G})$ .

**Proposition 6.** For a graph  $G = (V,E)$ ,  $\chi(A(\bar{G})) = \chi(A(G))$  if, and only if,  
i).  $G$  is of diameter 3 or ii).  $G$  is disconnected and the components of  $G$  are complete graphs.

**Corollary 7.** If  $G$  is a graph of diameter 2 and  $G$  is not disconnected then,  
 $\chi(A(\bar{G})) < \chi(A(G))$ .

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