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## Chromatic number of S-Antipodal Graph

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### Abstract

Chromatic number of a graph  $G$  is the minimum number of colors with which a graph can be colored properly and it is denoted by  $\chi(G)$ . In this paper we are finding the chromatic number of S-Antipodal graph, also we discussed the chromatic number of different properties of S-Antipodal graph.

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### I. INTRODUCTION:

#### Antipodal graph

Singleton (1968) introduced the concept of the Antipodal graph of a graph  $G$ , denoted by  $A(G)$ , is the graph on the same vertices as of  $G$ , two vertices being adjacent if the distance between them is equal to the diameter of  $G$ .

#### Chromatic number of Antipodal graph

By the motivation of existing definition of Chromatic number of a graph and Antipodal graph we can find the Chromatic number of Antipodal graph [1].

#### S-Antipodal graph

The eccentricity  $e(v)$  of a vertex  $v$  in the graph  $G$  is the distance to a vertex farthest from  $v$ . The maximum eccentricity is the diameter of  $G$  and the minimum is the radius of  $G$ . The center  $C(G)$  of a graph  $G$  is the set of vertices with minimum eccentricity.

A graph  $G$  is self centered, if all its vertices lie in the center. Equivalently, a self centered graph is a graph whose diameter equals to its radius.

Radhakrishnan Nair and Vijaykumar [5] introduced the concept of S-antipodal graph of a graph  $G$  as the graph  $A^*(G)$  has the vertices in  $G$  with maximum eccentricity and two vertices of  $A^*(G)$  are adjacent if they are at a distance of  $diam(G)$  in  $G$ .

#### Chromatic number of S-Antipodal graph

By the motivation of existing definition of Chromatic number of a graph and S-Antipodal graph we can find the Chromatic number of S-Antipodal graph. We consider only finite undirected graphs  $G = (V,E)$  without loops and multiple edges and follow Harary [3] for notation and terminology.

## II. RESULTS AND DISCUSSION:

**Proposition 1.** For a graph  $G$ ,  $\chi(G) = \chi(A^*(G))$  if, and only if  $G$  is complete or Hamiltonian  
 For any positive integer  $k$ , the  $k^{\text{th}}$  iterated  $S$ -antipodal graph  $A^*(G)$  is defined as follows:

$$(A^*)^0(G) = A^*(G), (A^*)^k(G) = A^*((A^*)^{k-1}(G))$$

**Corollary 2.** For any graph  $G$ , and any positive integer  $k$ ,  $\chi((A^*)^k(G)) = \chi(A^*(G))$

**Proposition 3. (Aravamudhan and Rajendran [5])** If  $G$  is a regular self- complementary graph, then  $A^*(G) = \bar{G}$

In view of the above, we have the following result:

**Proposition 4.** If  $G$  is a regular self- complementary graph, then  $\chi(A^*(G)) = \chi(\bar{G})$

**Proof.** Since  $G$  is regular self-complimentary graph, then by proposition3  $A^*(G) = \bar{G}$  that is  $A^*(G) \cong \bar{G}$  there is one to one correspondence between edges and vertices so,  $\chi(A^*(G)) = \chi(\bar{G})$

**Proposition 5. (Aravamudhan and Rajendran [5])**  $A^*(G) = A^*(\bar{G})$  if and only if  $G$  is either complete or totally disconnected

**Proposition 6.** For a graph  $G = (V,E)$ ,  $\chi(A^*(\bar{G})) = \chi(A^*(G))$  if, and only if,  $G$  is either complete or totally disconnected.

**Corollary 7.** If  $G$  is a graph of diameter 3 and  $G$  is not disconnected then,  
 $\chi(A^*(G)) < \chi(\bar{G})$ .

**Proposition 8. (Aravamudhan and Rajendran [5])** Let  $G$  be a graph,  $A(G)$  its antipodal graph and  $A^*(G)$  its  $S$ - Antipodal graph then  $A^*(G) = A(G)$  if and only if  $G$  is self centered.

**Proposition 9.** Let  $G$  be a graph,  $A(G)$  its antipodal graph then  $A^*(G)$  its  $S$ - Antipodal graph then  $\chi(A^*(G)) = \chi(A(G))$  if and only if  $G$  is self centered.

**Proof:** If  $G$  is self centered, then by proposition 8  $A^*(G) = A(G)$  that is  $A^*(G) \cong A(G)$  then  $A^*(G)$  and  $A(G)$  having one to one correspondence with vertices and edges hence  $\chi(A^*(G)) = \chi(A(G))$ .

If  $\chi(A^*(G)) = \chi(A(G))$  then  $A^*(G) \cong A(G)$  that is  $A^*(G) = A(G)$  by proposition 8  $G$  is self centered.

## III. CONCLUSION:

In this paper we compare the chromatic number of general graph and  $S$ -Antipodal graph and we conclude with some properties.

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