

USN

--	--	--	--	--	--	--	--	--	--

18EE63

Sixth Semester B.E. Degree Examination, Feb./Mar. 2022

Digital Signal Processing

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Prove the following properties of DFT.
i) Linearity ii) circular item shift. (06 Marks)
- b. Compute N-point DFT of $x(n) = a^n$ for $0 \leq n \leq N - 1$. (04 Marks)
- c. Compute 6-point DFT of the sequence $x(n) = \{4, 3, 2, 1, 0, 0\}$. Also plot magnitude and phase spectrum. (10 Marks)

OR

- 2 a. Compute the circular convolution using DFT and IDFT for the following sequences $x_1(n) = \{2, 1, 2, 1\}$ and $x_2(n) = \{1, 2, 3, 4\}$. (10 Marks)
- b. A long sequence $x(n)$ is filtered through a filter with impulse response $h(n)$ to yield to output $y(n)$. If $x(n) = \{1, 4, 3, 0, 7, 4, -7, -7, -1, 3, 4, 3\}$ and $h(n) = \{1, 2\}$. Compute $y(n)$ using overlap add technique. Use only a 5-point circular convolution in your approach. (10 Marks)

Module-2

- 3 a. Develop an 8-point DIT – FFT algorithm starting from the equation of DFT and also draw signal flow graph. (10 Marks)
- b. Obtain 8-point DFT of the following sequence using radix – 2 DIF-FFT algorithm. $x(n) = \{2, 1, 2, 1\}$. (10 Marks)

OR

- 4 a. First five points of the 8-point DFT of a real valued sequence is given by $X(0) = 0$, $X(1) = 2 + j2$, $X(2) = -j4$, $X(3) = 2 - j2$, $X(4) = 0$. Determine the remaining points. Hence find the original sequence $x(n)$ using DIF-FFT algorithm. (14 Marks)
- b. Tabulate the number of complex multiplications and complex additions required for the direct computation of DFT and FFT algorithm for $N = 8, 16, 32$. (06 Marks)

Module-3

- 5 a. Design an analog bandpass filter to meet the following frequency domain specifications :
i) a – 3.0103dB upper and lower cut-off frequency of 50Hz and 20KHz
ii) a stopband attenuation of atleast 20dB and 20Hz and 45KHz
iii) a monotonic frequency response. (10 Marks)
- b. Design a Chebyshev analog lowpass filter that has a –3dB cut-off frequency of 100rad/sec and a stopband attenuation of 25dB or greater for all radian frequencies past 250 rad/sec. (10 Marks)

OR

- 6 a. Determine the system function $H(z)$ of the lowest order Chebyshev filter that meets the following specifications :
i) 3dB ripple in the passband $0 \leq |\omega| \leq 0.3\pi$
ii) Atleast 20dB attenuation in the stopband $0.6\pi \leq |\omega| \leq \pi$
Use the bilinear transformation. (10 Marks)
- b. Transform the analog filter $H_a(s) = \frac{(s+1)}{s^2 + 5s + 6}$ into $H(z)$ using impulse invariant transformation take $T = 0.1$ sec. (10 Marks)

Module-4

- 7 a. A Chebyshev – I filter of order $N = 3$ and unit band width is known to have a pole at $s = -1$
- Find the two other poles of the filter and parameter ϵ
 - The analog filter is mapped to the z -domain using the bilinear transformation with $T = 2$. Find the transfer function $H(z)$ of the digital filter. (10 Marks)
- b. Design a digital Chebyshev-I filter that satisfies the following constraints :
- $$0.8 \leq |H(\omega)| \leq 1 \quad 0 \leq \omega \leq 0.2\pi$$
- $$|H(\omega)| \leq 0.2 \quad 0.6 \leq \omega \leq \pi$$
- Use impulse invariant transformation. (10 Marks)

OR

- 8 Obtain the direct form-I, direct form-II, cascade and parallel form realization for the following system :
- $$y(n) = 0.75y(n-1) - 0.125y(n-2) + 6x(n) + 7x(n-1) + x(n-2). \quad (20 \text{ Marks})$$

Module-5

- 9 a. A low pass filter is to be designed with the following desired frequency response

$$H_d(e^{j\omega}) = H_d(\omega) = \begin{cases} e^{-j2\omega}, & |\omega| < \pi/4 \\ 0, & \pi/4 < |\omega| < \pi \end{cases}$$

Determine the filter co-efficient $h_d(n)$ and $h(n)$ if $\omega(n)$ is a rectangular window defined as

$$\omega_R(n) = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{otherwise} \end{cases}$$

Also find the frequency response $H(\omega)$ of the resulting filter. (10 Marks)

- b. Use the window method with a hamming window to design a 7-tap differentiator. The magnitude response of an ideal differentiator is shown in Fig.Q9(b). Compute and plot the magnitude response of the resulting FIR differentiator.

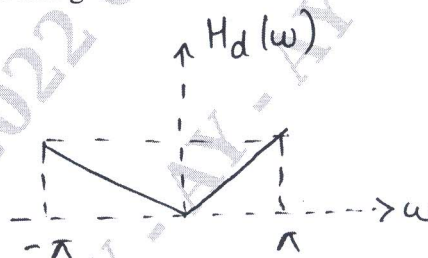


Fig.Q9(b)

(10 Marks)

OR

- 10 a. Determine the impulse response $h(n)$ of a filter having desired frequency response :

$$H_d(e^{j\omega}) = \begin{cases} e^{-j(N-1)\omega/2} & \text{for } 0 \leq |\omega| \leq \pi/2 \\ 0, & \text{for } \pi/2 \leq |\omega| \leq \pi \end{cases}$$

$N = 7$. Use frequency sampling approach. (12 Marks)

- b. Obtain direct form and cascade form realization of the system function :

$$H(z) = 1 + \frac{5}{2}z^{-1} + 2z^{-2} + 2z^{-3}. \quad (08 \text{ Marks})$$
