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10MT74

Seventh Semester B.E. Degree Examination, Feb./Mar. 2022  
**Digital Signal Processing**

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting atleast TWO questions from each part.

PART - A

- 1 a. Explain frequency domain sampling and reconstruction of DT signals. (10 Marks)
- b. Find the 4-point DFT of the sequence  $x(n) = \cos\left(\frac{n\pi}{4}\right)$ . (04 Marks)
- c. Explain the relationship between :  
i) DFT and Z - transform  
ii) DFT and DTFT. (06 Marks)
- 2 a. Compute the circular convolution of  $x_1(n) = \{2, 1, 2, 1\}$ ;  $x_2(n) = \{1, 2, 3, 4\}$  using DFT and IDFT method. (06 Marks)
- b. State and prove :  
i) Circular time shift property  
ii) Parseval's theorem. (06 Marks)
- c. Find the output  $y(n)$  of a filter with impulse response  $h(n) = \{1, 2\}$  and input signal  $x(n) = \{1, 2, -1, 2, 3, -2, -3, -1, 2, -1\}$  using overlap save method. [Use 4-point circular convolution in your approach]. (08 Marks)
- 3 a. Tabulate the number of complex multiplications and complex additions required for direct computation of DFT and FFT algorithms for  $N = 8, 32, 512, 1024$ . (10 Marks)
- b. Compute the circular convolution using DIT - FFT algorithm.  
 $x_1(n) = \{2, 3, 1, 1\}$ ,  $x_2(n) = \{1, 3, 5, 3\}$ . (10 Marks)
- 4 a. Derive the radix-2 DIT - FFT algorithm for  $N = 8$  and draw the signal flow graph. (10 Marks)
- b. If  $x(n) = \{2, 1, 2, 1\}$  compute 8-point DFT of  $x(n)$  using DIF - FFT algorithm. (10 Marks)

PART - B

- 5 a. Design an analog filter with maximally flat response in the passband and an acceptable attenuation of -2dB at 20rad/sec. The attenuation in the passband should be more than 10dB beyond 30rad/sec. (10 Marks)
- b. Design a lowpass 1rad/sec bandwidth Chebyshev filter with the following characteristics :  
i) Acceptable passband ripple of 2dB  
ii) Cut-off radian frequencies of 1 rad/sec  
iii) Stopband attenuation of 20dB or greater beyond 1.3rad/sec. (10 Marks)

- 6 a. Design a FIR filter for the desired frequency response of a lowpass filter given by

$$H_d(e^{j\omega}) = e^{-j2\omega} \quad \text{for} \quad -\frac{\pi}{4} \leq \omega \leq \frac{\pi}{4}$$

$$0 \quad \text{for} \quad \frac{\pi}{4} \leq |\omega| \leq \pi$$

Using rectangular window of length 5. (10 Marks)

- b. Determine the impulse response  $h(n)$  of a filter having desired frequency response.

$$H_d(e^{j\omega}) = e^{-j(N-1)\omega/2} \quad \text{for} \quad 0 \leq |\omega| \leq \frac{\pi}{2}$$

$N = 7$ , use frequency sampling approach. (10 Marks)

- 7 a. Design the Chebyshev filter using bilinear transformation to meet the following specification :

$$0.707 \leq |H(e^{j\omega})| \leq 1 \quad 0 \leq \omega \leq 0.2\pi$$

$$|H(e^{j\omega})| \leq 0.1 \quad 0.5\pi \leq \omega \leq \pi$$

(14 Marks)

- b. Find the  $H_a(s) = \frac{1}{(s+1)(s+2)}$  corresponding  $H(z)$  using impulse invariance method for sampling frequency of 5 samples/sec. (06 Marks)

- 8 a.  $H(z) = \frac{1 + \frac{1}{5}z^{-1}}{\left(1 - \frac{1}{2}z^{-1} + \frac{1}{3}z^{-2}\right)\left(1 + \frac{1}{4}z^{-1}\right)}$ . Realize direct form 1 and cascade. (08 Marks)

- b. Realize using linear phase  $H(z) = \frac{1}{2} + \frac{1}{3}z^{-1} + z^{-2} + \frac{1}{4}z^{-3} + z^{-4} + \frac{1}{3}z^{-5} + \frac{1}{2}z^{-6}$ . (04 Marks)

- c. Consider a FIR filter with system function,  $H(z) = 1 + 2.82z^{-1} + 3.4048z^{-2} + 1.74z^{-3}$ , sketch the lattice realization of the filter. (08 Marks)

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