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15AU73

Seventh Semester B.E. Degree Examination, July/August 2022
Finite Element Modeling and Analysis

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- Derive the equilibrium equation for 3D elastic body. (08 Marks)
 - Explain the with neat sketch plane stress and plane strains. (08 Marks)

OR

- State the principles of minimum potential energy. Explain the potential energy with usual notations. (08 Marks)
 - By RR method for a bar of Cross section area A, elastic modulus E, subjected to uniaxial loading P. Show that a distance X from fixed end is $u = \left(\frac{P}{AE}\right)X$. (08 Marks)

Module-2

- For the spring system shown in Fig.Q3(a) using principle of minimum potential energy. Determine the nodal displacement. Take $F_1 = 75N$ and $F_2 = 100N$.

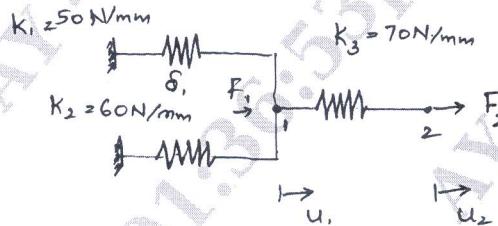


Fig.Q3(a)

- What is FEM? What are the advantages and limitations? (08 Marks)

OR

- What do you understand FEM? Briefly explain the steps involved in FEM. (08 Marks)
 - Derive the stiffness matrix for the bar subjected to axial load F using direct method. (08 Marks)

Module-3

- Determine the nodal displacement stress in each element and support reaction in the bar shown in Fig.Q5(a).

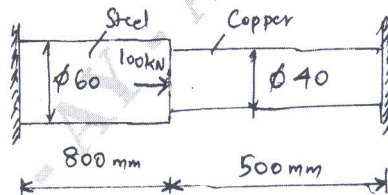


Fig.Q5(a)

$$P = 100 \text{ kN}$$

$$E_{\text{Steel}} = 200 \text{ GPa}$$

$$E_{\text{Cu}} = 100 \text{ GPa}$$

- Solve the following system of simultaneous equation by Gauss Elimination method.

$$\begin{aligned} x + y + z &= 9 \\ x - 2y + 3z &= 8 \\ 2x + y - z &= 3. \end{aligned}$$

(08 Marks)

OR

- 6 a. For the two bar truss shown in Fig.Q6(a). Determine the nodal displacement. Take $E = 2 \times 10^5 \text{MPa}$, $A = 200 \text{mm}^2$.

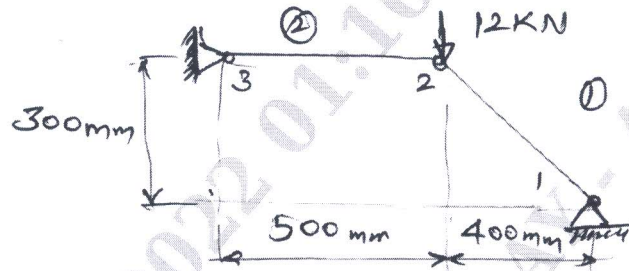


Fig.Q6(a)

(08 Marks)

- b. Derive the elemental stiffness matrix for a truss element.

(08 Marks)

Module-4

- 7 a. Derive the shape function using Lagrangian interpolation for liner quadrilateral element.

(08 Marks)

- b. Briefly explain Sub parametric element and Super parametric elements.

(08 Marks)

OR

- 8 a. Derive the Hermite shape function for a 2 noded beam element.

(08 Marks)

- b. Briefly explain the finite element formulation of 2D Constant Stream Triangle (CST).

(08 Marks)

Module-5

- 9 a. Fig.Q9(a) shown in simply supported beam subjected to a uniformly distributed load. Obtain the maximum deflection. Take young's modulus $E = 200 \text{GPa}$ and moment of inertia $I = 2 \times 10^6 \text{mm}^4$.

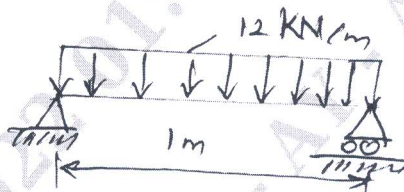


Fig.Q9(a)

(08 Marks)

- b. Derive differential equation for an 1D heat conduction.

(08 Marks)

OR

- 10 a. Derive the expression for stiffness matrix for 1D heat conduction.

(08 Marks)

- b. Determine the temperature distribution in the rectangular fin shown in Fig.Q10(b). Neglect the convection heat transfer and assume heat generated inside the fin as 500W/m^3 .

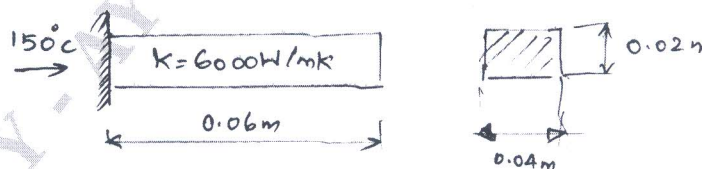


Fig.Q10(b)

(08 Marks)
