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17MT73

Seventh Semester B.E. Degree Examination, July/August 2022

Signal Process

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Explain the classification of signals :
- (i) Continuous time and discrete time signals.
 - (ii) Analog and Digital signal.
 - (iii) Deterministic and random signal.
 - (iv) Even and Odd signal.
 - (v) Periodic and Non periodic signals. (10 Marks)
- b. A discrete time signal $x(n]$ is described by,

$$x(n] = \begin{cases} 1 & n \geq 1, 2, 3 \\ -1 & n = -1, -2, -3 \\ 0 & n = 0, |n| > 3 \end{cases}$$

Find $y(n] = x(2n + 2)$. (10 Marks)

OR

- 2 a. Explain energy and power signal. Find the average power of the signal $x(n] = u(n]$, where $u(n]$ is shown in Fig. Q2 (a) below. (10 Marks)

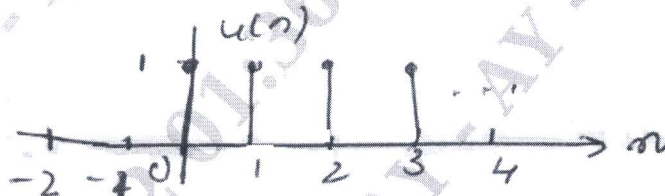


Fig. Q2 (a)

- b. Find the even and odd component of $x(t) = e^{jt}$. (04 Marks)
- c. A discrete time signal $x(n]$ is shown in Fig. Q2 (c). Sketch and label of following signals :
- (i) $x(n - 2)$
 - (ii) $x(2n)$
 - (iii) $x(-n)$

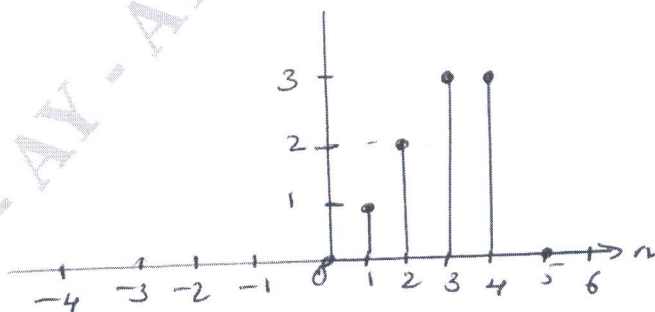


Fig. Q2 (c)

(06 Marks)

Module-2

- 3 a. Find the convolution sum of the 2 sequences $x_1(n)$ and $x_2(n)$ given below:

$$x_1(n) = (1, 2, 3)$$

$$x_2(n) = (2, 1, 4)$$

Also show that :

$$x(n) * \delta(n) = x(n)$$

$$x(n) * \delta(n - n_0) = x(n - n_0)$$

(10 Marks)

- b. An LTI system is characterised by an impulse response,

$$h(n) = \left(\frac{3}{4}\right)^n u(n)$$

Find the step response of the system. Also evaluate the output of the system $n = \pm 5$.

(10 Marks)

OR

- 4 a. With the relevant equations state and explain the convolutional integral. (10 Marks)

- b. Convolute the two continuous time signals $x_1(t)$ and $x_2(t)$ given below:

$$x_1(t) = \cos \pi t [u(t+1) - u(t-3)].$$

$$x_2(t) = \hat{u}(t)$$

(10 Marks)

Module-3

- 5 a. State the definition of Discrete Fourier Transform :

Compute the 8 point DFT of the sequence, $x(n) = (1, 1, 1, 1, 0, 0, 0, 0)$.

(10 Marks)

- b. Compute the DFT of the sequence defined by $x(n) = (-1)^n$ for,

(i) $N = 3$, (ii) $N = 4$, (iii) N odd, (iv) Never.

(10 Marks)

OR

- 6 a. Find the 8 point DFT of the sequence :

$$x(n) = (1, 2, 3, 4, 4, 3, 2, 1)$$

Using DIT-FFT radix 2 algorithm. The basic computational block known as the butterfly should be as shown in Fig. Q6 (a) below.

(12 Marks)

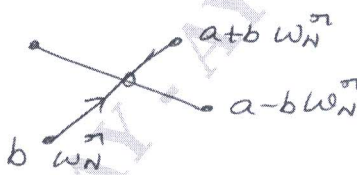


Fig. Q6 (a)

- b. Compute the 4 point DFT of the sequence $x(n) = (1, 0, 1, 0)$.

Also find $y(n)$ if $Y(K) = X((K - 2))_4$.

(08 Marks)

Module-4

- 7 a. A Butterworth low pass filter has to meet the following specifications:

(i) Passband gain $K_p = -1$ dB at $\Omega_p = 4$ rad/sec.

(ii) Stop band attenuation greater than or equal to 20 dB at $\Omega_s = 8$ rad/sec.

Determine the transfer function $H_a(S)$ of the lowest order Butterworth filter to meet the above specifications. (12 Marks)

- b. Find the order N of the following low pass Butterworth filter to meet the specifications :

$$\delta_p = 0.001, \delta_s = 0.001, \Omega_p = 1 \text{ rad/sec}, \Omega_s = x \text{ rad/sec.}$$

(08 Marks)

OR

- 8 a. A third order Butterworth low pass filter has the transfer function,

$$H(s) = \frac{1}{(s+1)(s^2+s+1)}$$

Design $H(z)$ using impulse invariant technique. (10 Marks)

- b. Determine the system function $H(z)$ of the lowest order Chebyshev filter that meets the following specifications :

i) 3 dB ripple in the passband $0 \leq |\omega| \leq 0.3\pi$.

ii) At least 20 dB attenuation in the stopband $0.6\pi \leq |\omega| \leq \pi$.

Use the bilinear transformation. (10 Marks)

Module-5

- 9 a. A low pass filter is to be designed with the following desired frequency response:

$$H_d(e^{j\omega}) = H_d(\omega) = \begin{cases} e^{-j2\omega}, & |\omega| < \frac{\pi}{4} \\ 0, & \frac{\pi}{4} < |\omega| < \pi \end{cases}$$

Determine the filter coefficients $h_d(n)$ and $h(n)$ if $\omega(n)$ is a rectangular window defined as follows:

$$\omega_r(n) = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{otherwise} \end{cases}$$

Also find frequency response $H(\omega)$ of the resulting FIR filter. (10 Marks)

- b. The frequency response of an FIR filter is given by,

$H(\omega) = e^{-j3\omega}(1 + 1.8\cos 3\omega + 1.2\cos 2\omega + 0.5\cos \omega)$ Determine the coefficients of the impulse response $h(n)$ of the FIR filter. (10 Marks)

OR

- 10 a. Draw the block diagram of direct form I and direct form II realizations for a digital IIR

filter described by system functions : $H(z) = \frac{8z^3 - 4z^2 + 11z - 2}{\left(\frac{z-1}{4}\right)\left(z^2 - z + \frac{1}{2}\right)}$. (10 Marks)

- b. Obtain a cascade realization for a system described by,

$$H(z) = \frac{1 + \frac{1}{4}z^{-1}}{\left(1 + \frac{1}{2}z^{-1}\right)\left(1 + \frac{1}{2}z^{-1} + \frac{1}{4}z^{-2}\right)}$$
 (10 Marks)
