

USN

Fourth Semester B.E. Degree Examination, Jan./Feb. 2023

Control Systems

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Define Control System. Distinguish between open loop and closed loop control systems. (06 Marks)
- b. Write the differential equations of performance for the mechanical system shown in Fig.Q1(b). Draw its F – V analogous circuit.

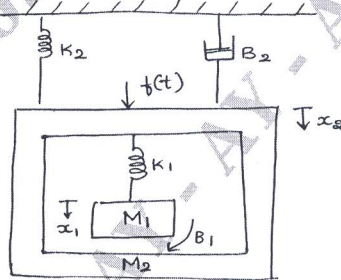


Fig.Q1(b)

(08 Marks)

- c. For the signal flow graph shown in Fig.Q1(c), determine the transfer function $\frac{C(s)}{R(s)}$ using Mason's gain formula.

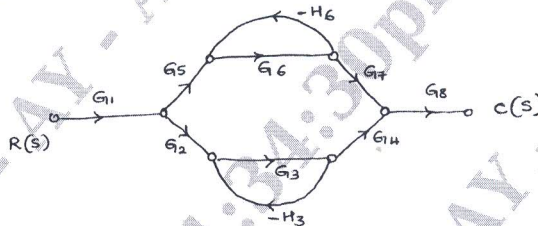


Fig.Q1(c)

(06 Marks)

OR

- 2 a. Illustrate how to perform the following in connection with block diagram reduction technique.
 - i) Shifting – take – off point after a summing point
 - ii) Shifting – take – off point before a summing point
 - iii) Removing minor feedback loop.(06 Marks)
- b. For the block diagram shown in Fig.Q2(b), determine the transfer function $C(s)/R(s)$ using block diagram reduction technique.

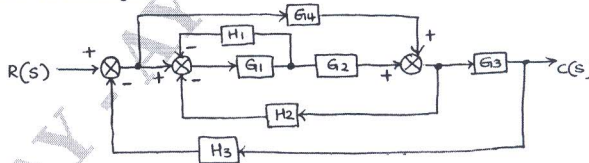


Fig.Q2(b)

(08 Marks)

- c. Obtain the transfer function $\frac{\theta_2(s)}{T(s)}$ for the system shown in Fig.Q2(c).

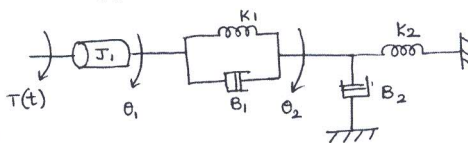


Fig.Q2(c)

(06 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and /or equations written eg. 42+8 = 50, will be treated as malpractice.

Module-2

- 3 a. Define the following time response specifications for an underdamped second order system :
- Rise time (t_r)
 - Peak time (t_p)
 - Peak overshoot (M_p)
 - Settling time (t_s).
- (04 Marks)
- b. A system is given by differential equation :
- $$\frac{d^2y(t)}{dt^2} + \frac{4dy(t)}{dt} + 8y(t) = 8x(t),$$
- where $y(t)$ is the output and $x(t)$ is the input. Determine all time domain specifications for unit step input assuming 2% criterion. (08 Marks)
- c. For a unity feedback system with $G(s) = \frac{s(s+1)}{s^2(s+3)(s+10)}$. Determine the type of the system, error co-efficient and steady state error for input $r(t) = 1 + 3t + \frac{t^2}{2}$. (08 Marks)

OR

- 4 a. Derive an expression for $c(t)$ of an underdamped second order system for a unit step input. (08 Marks)
- b. The unity negative feedback system with $G(s) = \frac{K(s+\alpha)}{(s+\beta)^2}$ is to be designed to meet the following specifications. Steady state error for a unit step input = 0.1, damping ratio = 0.5, natural frequency = $\sqrt{10}$ rad/sec. Find K , α and β . (08 Marks)
- c. Explain PID controller with the help of a block diagram. (04 Marks)

Module-3

- 5 a. State and explain Routh's stability criterion for determining the stability of the system. (04 Marks)
- b. Determine the number of roots that are :
- In the right half of s-plane
 - On the imaginary axis
 - In the left half of s-plane.
- For the system with the characteristic equation : $s^6 + 4s^5 + 3s^4 - 16s^2 - 64s - 48 = 0$. (08 Marks)
- c. The system shown in Fig.Q5(c) oscillates with a frequency of 2 rad/sec. Find the value of ' K_{mar} ' and ' P '. No poles are in RHS. (08 Marks)

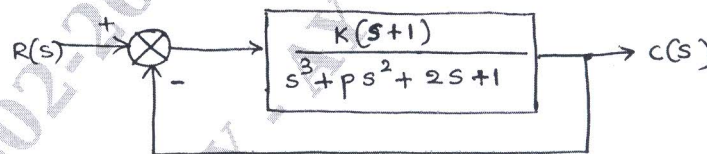


Fig.Q5(c)

(08 Marks)

OR

- 6 a. Explain the following rules with respect to root locus technique :
- Angle of asymptotes
 - Point of intersection with imaginary axis
 - Angle of departure.
- (06 Marks)
- b. The open loop transfer function of a control system is given by
- $$G(s)H(s) = \frac{K}{s(s+2)(s^2+6s+25)}$$
- Draw the complete root locus of the system. (14 Marks)

Module-4

- 7 a. Find the gain margin and phase margin for the negative feedback control system with an open loop transfer function :

$$G(s)H(s) = \frac{200}{s(s^2 + 12s + 100)} \quad (08 \text{ Marks})$$

- b. Construct the Bode plot for a unity feedback control system with

$$G(s)H(s) = \frac{10(s+10)}{s(s+2)(s+5)}$$

Find its gain margin and phase margin comment on the stability. (12 Marks)

OR

- 8 a. Explain the procedure for investigating the stability using Nyquist criterion. (06 Marks)
 b. For the system with open loop transfer function :

$$G(s)H(s) = \frac{10}{s^2(1+0.25s)(1+0.5s)}$$

Sketch the Nyquist plot and determine whether the system is stable or not? (14 Marks)

Module-5

- 9 a. Draw the block diagram of a typical system with digital controller and explain. (06 Marks)
 b. Obtain the state model of an electrical system shown in Fig.Q9(b).

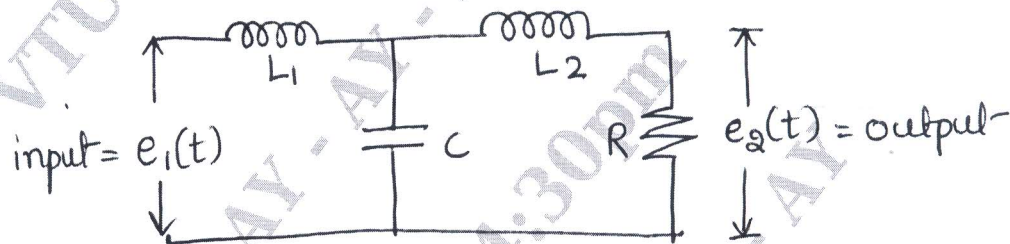


Fig.Q9(b)

(06 Marks)

- c. Find the transfer function of the system with a state model.

$$\begin{bmatrix} \dot{X}_1 \\ \dot{X}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} U \text{ and } y = [1 \ 0] \begin{bmatrix} X_1 \\ X_2 \end{bmatrix} \quad (08 \text{ Marks})$$

OR

- 10 a. State the properties of state transition matrix. (06 Marks)
 b. Obtain the state model for the system represented by the differential equation :

$$\frac{d^3y(t)}{dt^3} + \frac{9d^2y(t)}{dt^2} + \frac{26dy(t)}{dt} + 24y(t) = 6u(t) \quad (06 \text{ Marks})$$

- c. Find the state transition matrix for :

$$A = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \quad (08 \text{ Marks})$$

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