

CBCS SCHEME

BMATM101

USN

First Semester B.E./B.Tech. Degree Examination, Jan./Feb. 2023 Mathematics – I for Mechanical Engineering Stream

Time: 3 hrs.

Max. Marks: 100

- Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.
2. VTU Formula Hand Book is permitted.
3. M : Marks , L: Bloom's level , C: Course outcomes.*

| Module – 1 | | | M | L | C |
|-------------------|----|--|---|----|-----|
| Q.1 | a. | With usual notations prove that $\tan \phi = \frac{rd\theta}{dr}$. | 6 | L2 | CO1 |
| | b. | Find the pedal equation of $r^n = a^n \cos n\theta$ | 7 | L2 | CO1 |
| | c. | Find the angle of intersection of the curves $r = a(1 + \cos \theta)$, $r = b(1 - \cos \theta)$ | 7 | L2 | CO1 |
| OR | | | | | |
| Q.2 | a. | Derive the radius of curvature for the Cartesian curve. | 7 | L2 | CO1 |
| | b. | Find the angle between the polar curves $r = a \log \theta$, $r = \frac{a}{\log \theta}$ | 8 | L2 | CO1 |
| | c. | Using modern mathematical tool write a program/code to plot sine and cosine curves. | 5 | L3 | CO5 |
| Module – 2 | | | | | |
| Q.3 | a. | Expand $\sqrt{1 + \sin 2x}$ by Maclaurin's series upto the terms containing x^4 . | 6 | L2 | CO2 |
| | b. | If $U = f(x - y, y - z, z - x)$, show that $\frac{\partial U}{\partial x} + \frac{\partial U}{\partial y} + \frac{\partial U}{\partial z} = 0$. | 7 | L2 | CO2 |
| | c. | Examine the function $f(x, y) = x^3 + 3xy^3 + 15x^2 - 15y^2 + 72x$ for extreme values. | 7 | L3 | CO2 |
| OR | | | | | |
| Q.4 | a. | Evaluate $\lim_{x \rightarrow 0} \left(\frac{a^x + b^x + c^x + d^x}{4} \right)^{\frac{1}{x}}$. | 6 | L2 | CO2 |
| | b. | If $U = x^2 + y^2 + z^2$, $V = xy + yz + zx$, $W = x + y + z$, find $\frac{\partial(U, V, W)}{\partial(x, y, z)}$. | 7 | L2 | CO2 |
| | c. | Using modern mathematical tool to write a program/code to evaluate $\lim_{x \rightarrow \infty} \left(1 + \frac{1}{x} \right)^x$ | 7 | L3 | CO5 |
| Module – 3 | | | | | |
| Q.5 | a. | Solve $\frac{dy}{dx} + \frac{y \cos x + \sin y + y}{\sin x + x \cos y + x} = 0$. | 6 | L2 | CO3 |
| | b. | If the air is maintained at 30°C and the temperature of the body cools from 80°C to 60°C in 12 minutes, Find the temperature of the body after 24 minutes. | 7 | L3 | CO3 |
| | c. | Find the general and singular solutions of $xp^2 + xp - yp + 1 - y = 0$. | 7 | L2 | CO3 |

OR

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|-----|----|--|---|----|-----|
| Q.6 | a. | Solve $\frac{dy}{dx} + x \sin 2y = x^3 \cos^2 y$. | 6 | L2 | CO3 |
| | b. | Show that the parabola $y^2 = 4a(x + a)$ is self orthogonal. | 7 | L3 | CO3 |
| | c. | Solve $xyp^2 - (x^2 + y^2)p + xy = 0$. | 7 | L2 | CO3 |

Module - 4

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|-----|----|--|---|----|-----|
| Q.7 | a. | Solve $(D^4 - 4D^3 + 8D^2 - 8D + 4)y = 0$. | 6 | L2 | CO3 |
| | b. | Solve $(D^2 - 6D + 9)y = 6e^{3x} + 7e^{-2x} - \log 2$. | 7 | L2 | CO3 |
| | c. | Solve by variation of parameters $(D^2 + 1)y = \sec x$. | 7 | L2 | CO3 |

OR

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|-----|----|---------------------------------------|---|----|-----|
| Q.8 | a. | Solve $(D^2 - 4D + 13)y = \cos 2x$. | 6 | L2 | CO3 |
| | b. | Solve $y'' + 3y' + 2y = 12x^2$. | 7 | L2 | CO3 |
| | c. | Solve $(x^2)y'' - xy' + y = \log x$. | 7 | L2 | CO3 |

Module - 5

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|-----|----|--|---|----|-----|
| Q.9 | a. | Find the rank of the matrix $\begin{bmatrix} 1 & 2 & 3 & 1 \\ 2 & 1 & -1 & 0 \\ 3 & 3 & 2 & 1 \\ 2 & 4 & 6 & 2 \end{bmatrix}$ | 6 | L2 | CO4 |
| | b. | For what values λ and μ the system equations, $2x + 3y + 5z = 9$, $7x + 3y - 2z = 8$, $2x + 3y + \lambda z = \mu$, has i) No solution ii) a unique solution iii) infinite number of solutions. | 7 | L2 | CO4 |
| | c. | Solve the system of equations using Gauss Seidel method by taking $(0, 0, 0)$ as an initial conditions $10x + y + z = 12$, $x + 10y + z = 12$, $x + y + 10z = 12$. | 7 | L2 | CO4 |

OR

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|------|----|--|---|----|-----|
| Q.10 | a. | Using Gauss - Jordan method, solve $x + y + z = 11$, $3x - y + 2z = 12$, $2x + y - z = 3$. | 7 | L2 | CO4 |
| | b. | Using Rayleigh's power method find the dominant eigen value and the corresponding eigen vector of $\begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$ by taking $[1 \ 0 \ 0]^T$ as the initial eigen vector. [Carry out 6 iterations]. | 8 | L2 | CO4 |
| | c. | Using modern mathematical tool write a program/code to test the consistency of the equations $x + 2y - z = 1$, $2x + y + 4z = 2$, $3x + 3y + 4z = 1$. | 5 | L3 | CO5 |
