

18EE54

Fifth Semester B.E. Degree Examination, June/July 2023 Signals and Systems

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

a. Define signal and system. Explain real-life examples for each.

(08 Marks)

- b. Prove that:
 - i) $\int_{-a}^{a} x(t)dt = 2 \int_{0}^{a} x(t)dt$; if x(t) is even

ii)
$$\int_{-a}^{a} x(t)dt = 0$$
; if $x(t)$ is odd

(12 Marks)

OR

- 2 a. Sketch the following elementary signals:
 - (i) Unit-step
- (ii) Unit-Impulse function
- (iii) Ramp-function
- (iv) Exponential damped sinusoidal
- (08 Marks)
- b. What is the average power of triangular wave shown in Fig.Q2(b)?

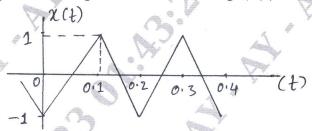


Fig.Q2(b) (12 Marks)

Module-2

a. Explain distributive property of convolution.

(10 Marks)

b. Find the forced response for the system described by

$$\frac{d^2y(t)}{dt^2} + 5\frac{dy(t)}{dt} + 6y(t) = 2x(t) + \frac{dx(t)}{dt} \quad \text{with input } x(t) = 2e^{-t}u(t)$$

OR

4 a. Explain associative property of convolution.

(10 Marks)

(10 Marks)

b. Find the zero-input response for the system described by the difference equation

$$y(n) + \frac{9}{16}y(n-2) = x(n-1)$$
 with initial conditions $y(-1) = 1$ and $y(-2) = -1$. (10 Marks)

Module-3

5 a. State and prove the Parsavel's theorem of CTFT.

(10 Marks)

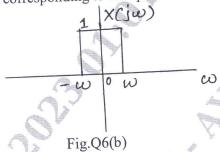
b. Obtain the Fourier transform of the signal, $x(t) = e^{-at}u(t)$; a > 0. Draw its magnitude and phase spectra. (10 Marks)

OR

State and prove Scaling property of CTFT.

(10 Marks)

b. Find the time-domain signal corresponding to the spectrum shown in Fig.Q6(b).



Module-4

(10 Marks)

State and prove frequency-differentiation property of DTFT.

(10 Marks)

Find the DTFT of the signal,

$$x(n) = \alpha^n u(n); |\alpha| < 1$$

Draw the magnitude spectrum.

(10 Marks)

State and prove symmetry property of DTFT.

(10 Marks)

Find the inverse DTFT of the following:

i)
$$X(e^{j\Omega}) = 1 + 2\cos\Omega + 3\cos2\Omega$$

ii) $Y(e^{j\Omega}) = j(3 + 4\cos\Omega + 2\cos2\Omega)\sin\Omega$

(10 Marks)

What are the properties of the region of convergence?

(10 Marks)

u(n-2) and sketch the Determine the z-transform and ROC for the signal x(n) = (10 Marks) ROC, poles and zeros in the z-plane.

OR

List the properties of Z-transform.

(10 Marks)

b. Find the inverse z-transform of

$$X(z) = \frac{z^3 + z^2 + \frac{3}{2}z + \frac{1}{2}}{z^3 + \frac{3}{2}z^2 + \frac{1}{2}z}; \quad \text{ROC: } |z| < \frac{1}{2}$$

by partial fraction expansion method.

(10 Marks)