

# CBCS SCHEME

15EE63

USN

--	--	--	--	--	--	--	--	--	--

## Sixth Semester B.E. Degree Examination, June/July 2023 Digital Signal Processing

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

### Module-1

- 1 a. Find the 4-point DFT of a sequence :

$$x(n) = \begin{cases} 1 & \text{for } 0 \leq n \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

Hence verify the result by taking IDFT using linear transformation.

(08 Marks)

- b. State and prove the following properties of DFT :

- Linearity
- Circular Time shift.

(08 Marks)

OR

- 2 a. Using overlap save method, compute  $y(n)$  of FIR filter with impulse response  $h(n) = \{1, 1, 1\}$  and input  $x(n) = \{1, 2, 0, -3, 4, 2, -1, 1, -2, 3, 2, 1, -3\}$ .

(08 Marks)

- b. The first 5 points of the 8 point DFT of a real valued sequence are :

$$\{0.25, 0.125 - j0.3018, 0, 0.125 - j0.518, 0\}$$

Determine remaining 3 points of the DFT. Estimate the value of  $x(0)$ .

(04 Marks)

- c. Compare linear and circular convolution.

(04 Marks)

### Module-2

- 3 a. What is FFT? Determine the number of multiplications and additions required for direct computation of DFT versus the FFT algorithm for  $N = 128$ .

(04 Marks)

- b. Given the sequences  $x_1(n) = \{1, 2, 3, 4\}$  and  $x_2(n) = \{4, 3, 2, 1\}$ . Compute the circular convolution for  $N = 4$  by using DIT - FFT algorithm.

(12 Marks)

OR

- 4 a. Find the DFT of  $x(n) = \{2, 1, 2, 1, 1, 2, 1, 2\}$  using the DIF - FFT algorithm.

(08 Marks)

- b. Develop a decimation in time algorithm for evaluating the DFT for  $N = 6$ .

(08 Marks)

### Module-3

- 5 a. For the given specifications  $K_p = 3\text{dB}$  ;  $K_g = 15\text{dB}$ ;  $\Omega_p = 1000\text{rad/sec}$ ;  $\Omega_s = 500\text{rad/sec}$ . Design analog Butterworth high pass filter.

(08 Marks)

- b. The system function of an analog filter is given as  $H_a(s) = \frac{1}{(s+1)(s+2)}$ , obtain  $H(z)$  using impulse invariant method. Take sampling frequency of 5 samples/sec.

(08 Marks)

OR

- 6 a. Design a Chebyshev filter to meet the following specifications :
- i) pass band ripple :  $\leq 2\text{db}$
  - ii) pass band edge :  $1\text{rad/sec}$
  - iii) stop band attenuation :  $\geq 20\text{db}$
  - iv) stop band edge :  $1.3\text{rad/sec}$ . (10 Marks)
- b. Convert the analog filter into a digital filter whose system function is
- $$H(s) = \frac{2}{(s+1)(s+3)}$$
- using bilinear transformation with
- $T = 0.1\text{sec}$
- . (06 Marks)

**Module-4**

- 7 a. Design the digital filter using Chebyshev approximation and bilinear transformation to meet the following specifications :
- Pass band ripple =  $1\text{dB}$  for  $0 \leq \omega \leq 0.15\pi$
  - Stop band attenuation  $\geq 20\text{dB}$  for  $0.45\pi \leq \omega \leq \pi$ . (12 Marks)
- b. Realize the following system function in cascade form :

$$H(z) = \frac{1 + \frac{1}{5}z^{-1}}{\left(1 - \frac{1}{2}z^{-1} + \frac{1}{3}z^{-2}\right)\left(1 + \frac{1}{4}z^{-2}\right)}$$
 (04 Marks)

OR

- 8 Obtain the direct form – I, direct form – II, cascade and parallel for the following system:
- $$y(n) = 0.75y(n-1) - 0.125y(n-2) + 6x(n) + 7x(n-1) + x(n-2).$$
- (16 Marks)

**Module-5**

- 9 a. What are the advantages and disadvantages with the design of FIR filters using window function? (06 Marks)
- b. Design a FIR low pass filter with the frequency response, using rectangular window :

$$hd(\omega) = \begin{cases} e^{-j\omega_c(N-1)/2} & -\frac{\pi}{2} \leq \omega \leq \frac{\pi}{2} \\ 0 & \text{elsewhere} \end{cases}$$
 (10 Marks)

OR

- 10 a. Distinguish between FIR and IIR filters. (04 Marks)
- b. Realize the FIR linear phase filter, with the impulse response,
- $$h(n) = \delta(n) - \frac{1}{2}\delta(n-1) + \frac{1}{4}\delta(n-2) + \frac{1}{4}\delta(n-3) - \frac{1}{2}\delta(n-4) + \delta(n-5).$$
- (06 Marks)
- c. Explain why windows are necessary in FIR filter design. What are the different windows in practice? (06 Marks)

\*\*\*\*\*