



## Fourth Semester B.E. Degree Examination, June/July 2023 Control Systems

Time: 3 hrs.

Max. Marks: 100

**Note: Answer any FIVE full questions, choosing ONE full question from each module.**

### Module-1

1. a. Define control system. Briefly explain the requirements of a control system. (04 Marks)
- b. For the mechanical system shown in Fig.Q1(b). Draw :
  - i) Mechanical network
  - ii) Write the differential equations
  - iii) Force-voltage analog
  - iv) Force-current analog.

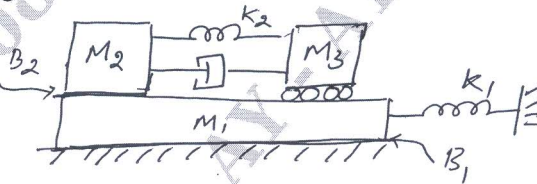


Fig.Q1(b)

(10 Marks)

- c. For the signal flow graph shown in Fig.Q1(c). Find the closed loop transfer function :

$$\frac{C(s)}{R(s)}$$

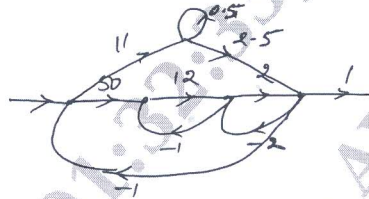


Fig.Q1(c)

(06 Marks)

### OR

2. a. Distinguish between open loop and closed loop control system with an example for each. (06 Marks)
- b. For the figure shown in Fig.Q2(a). Find the transfer function  $\frac{Q_2(s)}{T(s)}$ .

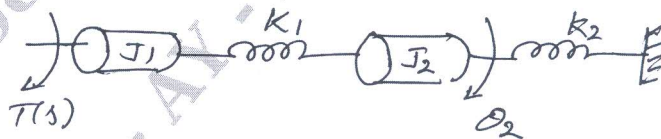


Fig.Q2(b)

(08 Marks)

- c. The system block diagram is given Fig.Q2(c), find  $\frac{C(s)}{R(s)}$ .

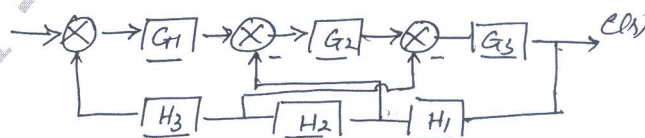


Fig.Q2(c)

(06 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.

**Module-2**

- 3 a. Derive an expression for the underdamped response of a second order feedback control system for step input. (06 Marks)
- b. A system is given by differential equation  $\frac{d^2y(t)}{dt^2} + 0.2 \frac{dy(t)}{dt} + y(t) = x(t)$ . determine time domain specifications for limit step input. (08 Marks)
- c. For a units feedback system having open loop transfer function :  

$$G(s) = \frac{120}{s^2(s+2)(s+3)}$$
 Determine steady state error for an input  $r(t) = 1 + 2 + 3t^2$ . (06 Marks)

**OR**

- 4 a. For a unity feedback system shown in Fig.Q4(a) find :  
 i) Percent over shoot for step input  
 ii) Settling time for step input  
 iii) Steady state error for input  $r(t) = 2 + 4t + 6t^2$ .

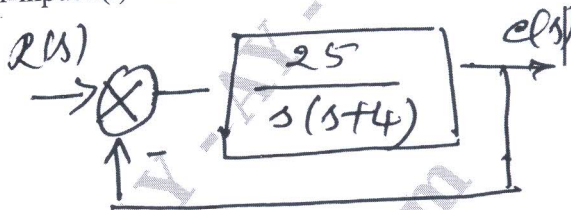


Fig.Q4(a)

(08 Marks)

- b. Find K and T for the system shown in Fig.Q4(b) such that the output response with unit step input.

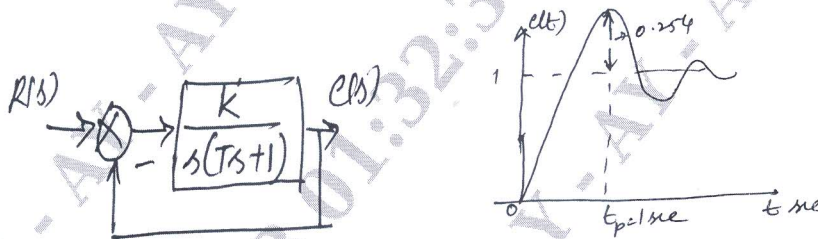


Fig.Q4(b)

(06 Marks)  
(06 Marks)

- c. Write a note on PID controllers.

**Module-3**

- 5 a. A feedback control system has characteristics equation  $s^5 - s^4 - 2s^3 + 2s^2 - 8s + 8 = 0$ .  
 How many poles are  
 i) Left half of s-plane  
 ii) On imaginary axis  
 iii) On the right half of s-plane. (05 Marks)
- b. A feedback control system has an open loop transfer function :  

$$G(s)H(s) = \frac{K}{s(s^2 + 6s + 10)}$$
 Sketch the root locus as K is varied from 0 to  $\infty$ . (10 Marks)
- c. Show that the root locus with  $G(s)H(s) = \frac{K(s+3)}{s(s+2)}$  is a circle having center (-3, 0) and radius  $\sqrt{3}$ . (05 Marks)

OR

- 6 a. For a system equation  $s^4 + 2s^3 + (4+k)s^2 + 9s + 25 = 0$ . Determine the K for system to be stable. (05 Marks)
- b. A feedback control system has an open loop transfer function :

$$G(s)H(s) = \frac{K}{s(s+4)(s^2+4s+20)}$$

Sketch the root locus as K is varied from 0 to  $\infty$ . (10 Marks)

- c. A feedback control system has an open loop transfer function :

$$G(s)H(s) = \frac{K}{s(s+3)(s^2+3s+11.25)}$$

Check if  $s = -1.5$  and  $s = -1.5 + 1.8375j$  is on the root locus. Use angle condition. (05 Marks)

**Module-4**

- 7 a. A unity feedback system is shown in Fig.Q7(a) find resonant peak, resonant frequency and phase shift.

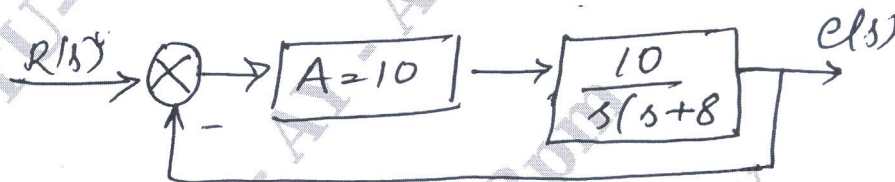


Fig.Q7(a)

- b. Draw the polar plot whose open loop transfer function is :

$$G(s)H(s) = \frac{1}{1+0.1s}$$

- c. The open loop transfer function :

$$G(s)H(s) = \frac{K}{s(1+0.02s)(1+0.05s)}$$

Draw the bode plot and from the diagram find the value of K for gain margin = 10dB. (10 Marks)

OR

- 8 a. Explain lead-lag compensator networks. (05 Marks)
- b. Using Nyquist stability investigate the closed loop stability for open loop transfer function:

$$G(s)H(s) = \frac{100}{(s+1)(s+2)(s+3)}$$

- c. The open loop transfer function  $G(s)H(s) = \frac{100}{s(s+5)(s+10)}$ . Draw the bode plot and from the diagram obtain gain margin and phase margin. (08 Marks)

Module-5

- 9 a. Define :
- State
  - State variable
  - State space
  - State transition matrix

(06 Marks)

- b. Find the state transition matrix of  $A = \begin{bmatrix} 0 & -1 \\ 2 & -3 \end{bmatrix}$ .

(08 Marks)

- c. Obtain the transfer function form the state model.

$$\begin{bmatrix} \dot{x}_1(t) \\ \dot{x}_2(t) \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -6 & -5 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t) \text{ and } y(t) = \begin{bmatrix} 8 & 1 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix}$$

(06 Marks)

OR

- 10 a. State the properties of state transition matrix.  
b. Obtain the state model for the system refer Fig.Q10(b).

(06 Marks)

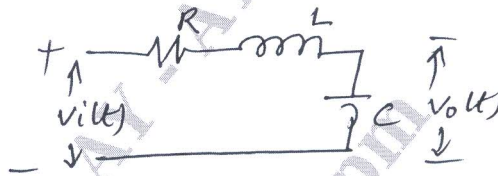


Fig.Q10(b)

(08 Marks)

- c. Represent the differential equation given below in a state model :

$$\frac{d^3 y(t)}{dt^3} + 3 \frac{d^2 y(t)}{dt^2} + \frac{6 dy(t)}{dt} + 7y(t) = 2u(t)$$

(06 Marks)

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