

21EC54

Fifth Semester B.E. Degree Examination, June/July 2024 Electromagnetic Waves

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

a. State and explain Coulomb's law of force between two point charges in vector form and mention the units of quantities in the force equation. (06 Marks)

b. Two point charge Q_1 and Q_2 are located at (1, 2, 0)m and (2, 0, 0)m respectively. Find the relation between the charges Q_1 and Q_2 such that the total force on a unit positive charge at (-1, 1, 0) have: i) No x-component ii) No y-component. (08 Marks)

c. List the expressions of electrified intensity É due to various charge distributions. (06 Marks)

OR

a. Derive the expression for eclectic field intensity (E) due to infinite line charge of uniform charge distribution and lies along the Z-axis.

b. Evaluate D (Electric flux density) at a point (6, 8,-10) due to:

i) A point charge of 40mC at the origin

ii) A uniform line charge of $\rho_L = 40 \mu C / m^2$ on the z-axis

iii) A uniform surface charge density of $\rho_s = 57.2 \mu C/m^2$ on the plane x = 12m. (08 Marks)

Module-2

3 a. State and prove Gauss's law for a point charge. (06 Marks)

b. The flux density within the cylindrical volume bounded by r = 5m, z = 0 to z = 2m is given by $\overrightarrow{D} = 30e^{-r}a_r - 2ZQ_zc/m^2$. Estimate the total outward flux crossing the surface of cylinder.

c. Define and derive the mathematical expression for divergence of a vector \overrightarrow{D} . (06 Marks)

OR

4 a. Given $D = 5ra_rc/m^2$, prove divergence theorem for a shell region enclosed by spherical surfaces @r = a and r = b (b > a) and centred @ the origin. (08 Marks)

b. Define electric potential. Obtain an expression for the potential difference between two points in an electric field. (06 Marks)

c. Drive current continuity equation.

(06 Marks)

Module-3

5 a. Find V at P(2, 1, 3) for the field of two co-axial conducting cones with V = 50V @ $\theta = 30^{\circ}$ and V = 20V @ @ $\theta = 50^{\circ}$. (06 Marks)

b. Derive Laplace and Poisson's equation from Gauss's law.

(06 Marks)

c. Use Laplace equation to find the capacitance per unit length of a co-axial cable of inner radius 'a'm and outer radius 'b'm. Assume $V = V_0 @ r = a$ and V = 0 @ r = b. (08 Marks)

OR

6 a. State and explain Biot-Savart's law.

(06 Marks)

- b. Give $H = 20r^2a\phi A/m$
 - i) Determine the current density (J).

(08 Marks)

- ii) Also determine the total current that crosses the surface r = 1 m, $0 < \phi < 2\pi$ and z = 0,
- c. Explain the concept of magnetic flux and magnetic flux density.

(06 Marks)

Module-4

- 7 a. A point charge of Q = -1.2C has velocity $\overrightarrow{V} = [5a_x + 2ay 3a_z]m/s$. Find the magnitude of the force exerted on the charge, if
 - i) $\vec{E} = -18a_x + 5a_y 10a_z v/m$
 - ii) $\vec{B} = -4a_x + 4a_y + 3a_z T$
 - iii) Both the field are present.

(08 Marks)

- b. Derive an expression for the force on a differential current element placed in a magnetic field.

 (07 Marks)
- c. State and explain Faraday's law of electromagnetic induction.

(05 Marks)

OR

- 8 a. Discuss the magnetic boundary conditions to apply to B and H at the interface between two different magnetic materials. (12 Marks)
 - b. If B=0.05xayT in a material for which $x_m=2.5$, find $\mu r,\,\mu,\,H,\,M,\,J,\,J_b.$

(08 Marks)

Module-5

- 9 a. Derive Maxwell's equation in integral and point form for time varying fields. (12 Marks)
 - b. Verify the field $\vec{E} = E_m \sin x \sin t \, a_y$ and $\vec{H} = \frac{E_m}{\mu_0} \cos x \cos t \, a_z \, \text{satisfy Maxwell's equations.}$

(08 Marks)

OR

- a. Determine the relation between E and H of an electromagnetic wave travelling in free space along z-direction. (10 Masks)
 - b. Discuss uniform plane wave propagating in a good conducting media and also explain the term skin depth. (10 Marks)

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