

CBCS SCHEME

18EC55

# Fifth Semester B.E. Degree Examination, June/July 2024 **Electromagnetic Waves**

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

## Module-1

State and derive Coulomb's law.

(06 Marks)

- b. Find the force on charge Q<sub>1</sub> located at (4, -2, 1) m due to charge Q<sub>2</sub> located at (3, -1, -2) m.  $Q_1 = 200 \mu C$ ,  $Q_2 = 300 \mu C$ . (07 Marks)
- c. Calculate the electric field intensity E at (-1, 3, -2) m due to infinite line charges with  $\rho_1 = 25 \text{ nC/m}$  lying along x-axis and  $\rho_1 = 50 \text{ nC/m}$  lying along y-axis. (07 Marks)

Derive electric field intensity E due to infinite line charge.

(06 Marks)

- Two point charges  $Q_1 = 5 \mu C$  and  $Q_2 = -3 \mu C$  are located in free space at (1, 0, -2) m and (-2, 1, 3) m respectively. Find electric field intensity E at P(-3, 2, -1) m. (07 Marks)
- c. Calculate the electric field intensity E at (-2, 1, -3) m due to infinite sheet charges:

$$\rho_s = \frac{1}{6\pi} \text{ nC/m}^2 \text{ located at y} = 3 \text{ m and}$$

$$\rho_s = \frac{1}{6\pi} \text{ nC/m}^2 \text{ located at y} = 3 \text{ m}$$

(07 Marks)

 $\rho_{S} = \frac{1}{3\pi} \text{ nC/m}^2 \text{ located at } z = -5 \text{ m}$ 

State and prove Gauss law.

(06 Marks)

- b. Given  $D = \frac{5r^3}{r} a_r C/m^2$  in cylindrical co-ordinates. Prove divergence theorem for the volume enclosed by r = 2m, r = 3m, z = 0 and z = 5m.
- Find the total charge in a volume defined by six planes for which,  $2 \le x \le 3$ ,  $3 \le y \le 4$ ,  $4 \le z \le 5$ , if  $D = 5x^2a_x + 4y^2a_y + 3za_z C/m^2$ .

- Using Gauss's law, derive the expressions for D and E due to co-axial cylindrical conductors.
  - b. Calculate the total electric flux density due to two uniform line charges of 30 μC/m lying along x-axis and 50  $\mu$ C/m lying along z-axis, at (2, 3, 4)m. (07 Marks)
  - In an electric field, potential field is  $V = 5x^2 + 3y^3 + 8z$  volts. Find
    - (i)
- (iii)  $\overline{D}$  at (-3, 2, 4) m

(07 Marks)

### Module-3

- Using Laplace's equation, derive the expression for potential (V) and electric field strength E due to two concentric cylinders of infinite length.
  - b. In spherical co-ordinates V = 750 volts at r = 25 cm and E = 825  $a_r$  V/m at r = 75 cm. Determine the location of voltage reference if potential depends only on r. (07 Marks)
  - State and prove Ampere's circuital law.

(07 Marks)

### OR

- 6 a. Using Biot-Savart's law, derive the expression for magnetic field intensity "H" due to infinite long conductor. (06 Marks)
  - b. In spherical co-ordinates, V = 0 for r = 0.2 m and V = 200 volts for r = 3 m. Assuming free space between concentric spheres (Shells) find electric field intensity E and flux density D. (07 Marks)
  - c. Find magnetic field intensity H at the center of a square loop of sides equal to 10 m and carrying a current of 5 amp. (07 Marks)

# Module-4

- 7 a. Derive the equation for magnetic force on a differential current element in a magnetic field. (06 Marks)
  - b. Calculate the force on a straight conductor of length 0.5 m carrying a current of 10 amp in the z-direction, where  $\overline{B} = 5 \times 10^{-3} a_x$  Tesla and  $B = 6 \times 10^{-3} a_y$  Tesla. (07 Marks)
  - c. A solenoid with air core has 2000 turns and a length of 700 mm. Core radius is 50 mm. Find self inductance. (07 Marks)

### OR

- 8 a. Derive the equation for force between two parallel current carrying conductors. (06 Marks)
  - b. Derive tangential and normal boundary conditions (magnetic) between two media of permeabilities  $\mu_1$  and  $\mu_2$ .
  - c. Find the inductance per unit length of a co-axial conductor with an inner radius of a=4 mm and outer radius of b=10 mm. Assume  $\mu_r=1$ . (07 Marks)

# Module-5

- 9 a. State the inconsistency of Ampere's law, for time varying fields. Derive Maxwell's equation to correct it. (06 Marks)
  - b. Derive general plane wave equation in terms of E, taking help of the Maxwell's equation (07 Marks)
  - c. A plane wave travelling in positive z-direction in a lossless unbounded medium has permeability 5 times that of free space and a dielectric constant 3 times that of free space.
    - (i) Find phase velocity of the wave
    - (ii) If E has only x-component with amplitude 25 V/m, find amplitude and direction of H. (07 Marks)

### OR

- 10 a. Prove that conduction current and displacement current are equal. (06 Marks)
  - b. State and explain Poynting theorem. (05 Marks)
  - c. Determine following parameters for a medium with  $\epsilon_r = 4$ ,  $\mu_r = 1$ ,  $\sigma = 20 \times 10^{-2} \, \text{S/m}$ ,  $f = 1 \, \text{mHz}$ .
    - (i) Attenuation constant
    - (ii) Phase shift constant
    - (iii) Propagation constant
    - (iv) Wavelength
    - (v) Phase velocity
    - (vi) Intrinsic impedance

(vii) Skin depth (δ)

(09 Marks)