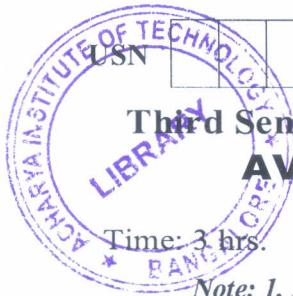


CBCS SCHEME

BMATEC301/BEC/BBM301



Third Semester B.E./B.Tech. Degree Examination, Dec.2023/Jan.2024

AV Mathematics – III for EC/BM Engineering

Time: 3 hrs.

Max. Marks: 100

Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.

2. M : Marks , L: Bloom's level , C: Course outcomes.

3. Statistical table and handbook permitted.

4. Use of VTU Mathematics handbook is permitted.

Module – 1			M	L	C
Q.1	a.	Obtain the Fourier series of $f(x) = \frac{\pi - x}{2}$ in $0 < x < 2\pi$. Hence deduce that $1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots = \frac{\pi}{4}$	6	L2	CO1
	b.	Expand $f(x) = 2x-1$ as a Cosine half range Fourier series in $0 < x < 1$.	7	L2	CO1
	c.	Compute the First harmonics of the Fourier series of $f(x)$. Given the table	7	L3	CO1

OR

Q.2	a.	Obtain the Fourier series of $f(x) = x $ in $(-\ell, \ell)$.	6	L2	CO1
	b.	Obtain the Cosine half range Fourier series of $f(x) = x^2$ in $0 < x < \pi$.	7	L3	CO1
	c.	Express Y as a Fourier Cosine series upto second harmonics. Given the table :	7	L3	CO1

x	0	2	4	6	8	10	12
y	9.0	18.2	24.4	27.8	27.5	22.0	9.0

Module – 2

Q.3	a.	Find the Fourier transform of $f(x) = e^{- x }$.	6	L2	CO2
	b.	Find the Fourier Cosine and Sine transform of $f(x) = e^{-ax}$, $a > 0$.	7	L3	CO2
	c.	i) Find a Discrete Fourier transform of the single $f = [3, 4, 5, 5]^T$. ii) Find the Inverse Discrete Fourier transform of the single obtained in part (i).	7	L3	CO2

OR

Q.4	a.	Find the Fourier transform of $f(x) = \begin{cases} 1- x & \text{for } x \leq 1 \\ 0 & \text{for } x > 1 \end{cases}$ and hence deduce that $\int_0^\infty \frac{\sin^2 t}{t^2} dt = \frac{\pi}{2}$.	6	L2	CO2
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	b.	Obtain the Fourier Cosine transform of $f(x) = \begin{cases} 4x & , 0 < x < 1 \\ 4-x & , 1 < x < 4 \\ 0 & , x > 4 \end{cases}$	7	L3	CO2
	c.	Solve the Integral equation $\int_0^{\infty} f(\theta) \cos \alpha \theta d\theta = \begin{cases} 1-\alpha & , 0 \leq \alpha \leq 1 \\ 0 & , \alpha > 1 \end{cases}$ and hence evaluate $\int_0^{\infty} \frac{\sin^2 t}{t^2} dt$.	7	L3	CO2

Module - 3

Q.5	a.	Find the Z – transform of i) $\cos n\theta$ ii) $\sin n\theta$.	6	L2	CO3
	b.	Find the Inverse Z – transform of $\frac{z^2 - 8z}{(z-4)^2}$.	7	L3	CO3
	c.	Solve the difference equation $y_{n+2} - 4y_n = 0$. Given that $y_0 = 0$ and $y_1 = 2$.	7	L3	CO3

OR

Q.6	a.	Find the Z – transform of $2n + \sin\left(\frac{n\pi}{4}\right) + 1$.	6	L2	CO3
	b.	Compute the Inverse Z – transform of $\frac{3z^2 + 2z}{(5z-1)(5z+2)}$.	7	L3	CO3
	c.	Solve the difference equation $u_{n+2} + 6u_{n+1} + 9u_n = 2^n$ with $u_0 = u_1 = 0$, using Z – transforms.	7	L3	CO3

Module - 4

Q.7	a.	Solve $(D^4 - m^4)y = 0$.	6	L2	CO4
	b.	Solve $(D^2 - 2D + 1)y = \sin x + e^x$.	7	L3	CO4
	c.	Solve $x \frac{d^3 y}{dx^3} + \frac{d^2 y}{dx^2} = \frac{1}{x}$.	7	L3	CO4

OR

Q.8	a.	Solve $\frac{d^3 y}{dx^3} + 8y = x^4 + 2x + 1$.	6	L2	CO4
	b.	Solve the Legendre's form of Linear equation. $(1+x)^2 \frac{d^2 y}{dx^2} + (1+x) \frac{dy}{dx} + y = \sin 2 [\log(1+x)]$.	7	L3	CO4
	c.	In the LCR circuit the charge q on a plate of condenser is given by $L \frac{d^2 q}{dt^2} + R \frac{dq}{dt} + \frac{q}{C} = E \sin pt$. Solve the above equation.	7	L3	CO4

Module – 5

Q.9	a.	Find a Least square straight line for the following data :	6	L2	CO5																																	
		<table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>x</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr> <tr><td>y</td><td>6</td><td>4</td><td>3</td><td>5</td><td>4</td><td>2</td></tr> </table>				x	1	2	3	4	5	6	y	6	4	3	5	4	2																			
x	1	2	3	4	5	6																																
y	6	4	3	5	4	2																																
b.	In a partially destroyed laboratory record, the lines of regression of y on x and x on y are available as $4x - 5y + 33 = 0$ and $20x - 9y = 107$. Calculate \bar{x} , \bar{y} and coefficient of correlation between x and y.																																					
	c.	Ten competition in a beauty contest are ranked by two judges A and B in the following order. Calculate the rank correlation coefficient. <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>ID No. of competition</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>Judge A</td><td>1</td><td>6</td><td>5</td><td>10</td><td>3</td><td>2</td><td>4</td><td>9</td><td>7</td><td>8</td></tr> <tr><td>Judge B</td><td>6</td><td>4</td><td>9</td><td>8</td><td>1</td><td>2</td><td>3</td><td>10</td><td>5</td><td>7</td></tr> </table>	ID No. of competition	1	2	3	4	5	6	7	8	9	10	Judge A	1	6	5	10	3	2	4	9	7	8	Judge B	6	4	9	8	1	2	3	10	5	7	7	L3	CO5
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Judge B	6	4	9	8	1	2	3	10	5	7																												
	OR																																					
Q.10	a.	Fit a parabola for the data in the form $y = ax^2 + bx + c$.	6	L2	CO5																																	
		<table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>x</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr> <tr><td>y</td><td>10</td><td>12</td><td>13</td><td>16</td><td>19</td></tr> </table>				x	1	2	3	4	5	y	10	12	13	16	19																					
x	1	2	3	4	5																																	
y	10	12	13	16	19																																	
b.	The following table gives the heights of Father (x) and Sons (y) : <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>x</td><td>65</td><td>66</td><td>67</td><td>67</td><td>68</td><td>69</td><td>70</td><td>72</td></tr> <tr><td>y</td><td>67</td><td>68</td><td>65</td><td>68</td><td>72</td><td>72</td><td>69</td><td>71</td></tr> </table> Find the lines of regression and hence calculate the co-efficient of correlation.	x	65	66	67	67	68	69	70	72	y	67	68	65	68	72	72	69	71																			
x	65	66	67	67	68	69	70	72																														
y	67	68	65	68	72	72	69	71																														
	c.	Determine the rank correlation for the following data which shows the marks obtained in two quizzes in mathematics.	7	L3	CO5																																	
		<table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>Marks in first quiz X</td><td>6</td><td>5</td><td>8</td><td>8</td><td>7</td><td>6</td><td>10</td><td>4</td><td>9</td><td>7</td></tr> <tr><td>Marks in first quiz Y</td><td>8</td><td>7</td><td>7</td><td>10</td><td>5</td><td>8</td><td>10</td><td>6</td><td>8</td><td>6</td></tr> </table>				Marks in first quiz X	6	5	8	8	7	6	10	4	9	7	Marks in first quiz Y	8	7	7	10	5	8	10	6	8	6											
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