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## Sixth Semester B.E./B.Tech. Degree Examination, Dec.2024/Jan.2025 Finite Element Methods

Time: 3 hrs.

Max. Marks: 100

*Note: Answer any FIVE full questions, choosing ONE full question from each module.*

### Module-1

- 1 a. Explain the following:
  - i) Work potential
  - ii) Strain energy

(04 Marks)
- b. Explain with neat sketch the simplex, complex and multiplex elements characteristics.
 

(06 Marks)
- c. Explain the basic steps involved in finite element method formulation.
 

(10 Marks)

OR

- 2 a. Explain the following:
  - i) Half band width
  - ii) Potential energy

(04 Marks)
- b. Explain the convergence criteria of a polynomial.
 

(06 Marks)
- c. Determine the expression for displacement in bar subjected to load P as shown in Fig.Q.2(c) by RR method.
 

(10 Marks)

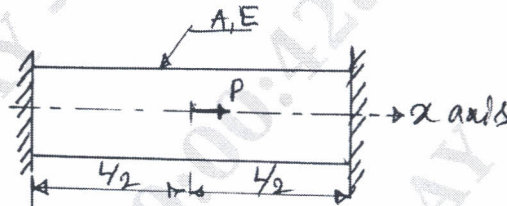


Fig.Q.2(c)

### Module-2

- 3 a. Derive the expression for shape functions of 3 noded triangular element with the help of polynomial approach in natural coordinate system.
 

(06 Marks)
- b. Define a shape function and list the properties of shape functions.
 

(04 Marks)
- c. Determine the nodal displacements and stress in each element of the bar shown in Fig.Q.3(c).
 

(10 Marks)

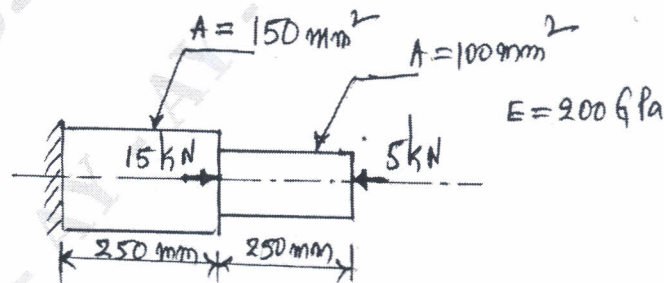


Fig.Q.3(c)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
2. Any revealing of identification, appeal to evaluator and /or equations written eg. 42+8 = 50, will be treated as malpractice.

OR

- 4 a. Derive the shape functions for a 8-noded quadrilateral element using Lagrangian method. (08 Marks)  
 b. Determine the nodal displacements for the truss system as shown in Fig.Q.4(b). (12 Marks)

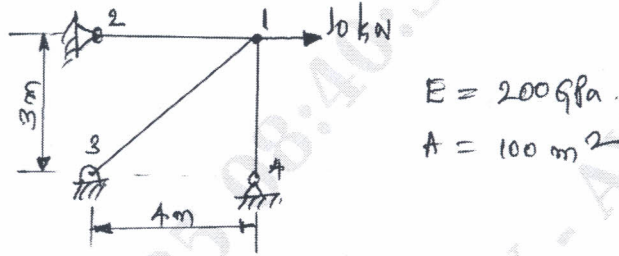


Fig.Q.4(b)

**Module-3**

- 5 a. Determine the global load vector for the beam as shown in Fig.Q.5(a). (06 Marks)

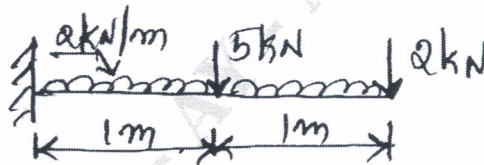


Fig.Q.5(a)

- b. Determine the deflection of the beam at its centre as shown in Fig.Q.5(b). (14 Marks)

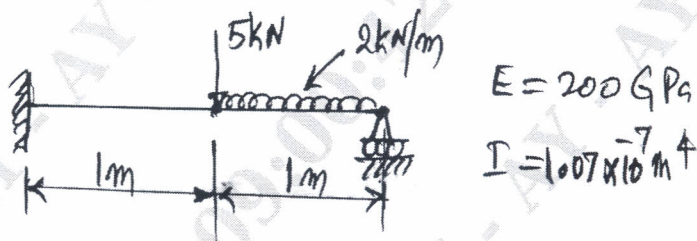


Fig.Q.5(b)

OR

- 6 a. Derive the stiffness matrix for torsion rod element. (06 Marks)  
 b. Determine the angle of twist at each end of section and shear stress in each section for torsion system shown in Fig.Q.6(b). (14 Marks)

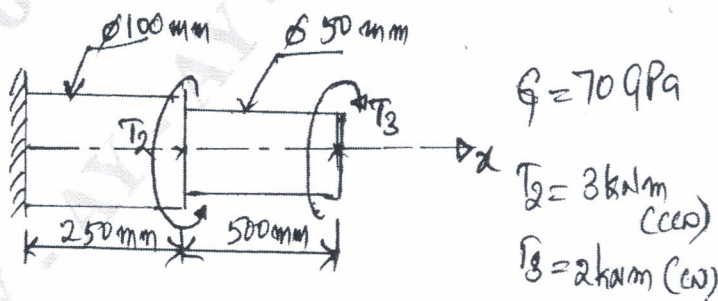


Fig.Q.6(b)

$G = 70 \text{ GPa}$   
 $T_2 = 3 \text{ kNm (CCW)}$   
 $T_3 = 2 \text{ kNm (CW)}$

**Module-4**

- 7 a. Derive the convection matrix for a round rod lateral surface, with usual notations. (06 Marks)  
 b. Determine the temperature distribution in a composite wall, as shown in Fig.Q.7(b), using 1 D formulation. (14 Marks)

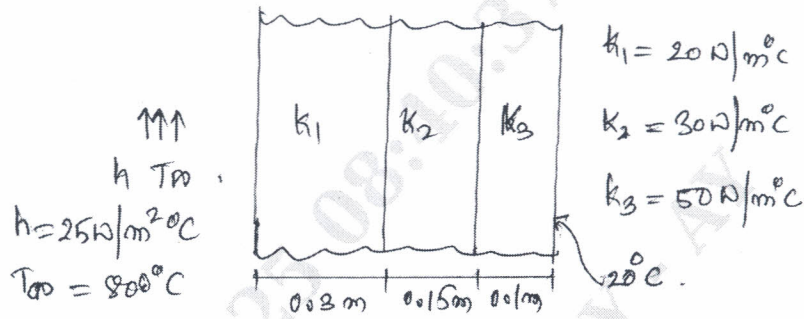


Fig.Q.7(b)

**OR**

- 8 a. Derive the conduction matrix [K] for 1D conduction with usual notations. (06 Marks)  
 b. A brick of wall thickness 0.3 m,  $K = 0.7 \text{ W/m}^\circ\text{C}$ , the inner surface is at  $28\text{°C}$  and outer surface is exposed to cool air of temperature  $-15\text{°C}$ . Determine the temperature distribution in brick and heat flux using two elements. (14 Marks)

**Module-5**

- 9 a. Explain 2D axi-symmetric element. (04 Marks)  
 b. Derive the strain-displacement matrix [B] for 2D axi-symmetric triangular element. (16 Marks)

**OR**

- 10 a. Write a note:  
 i) Lumped mass matrix  
 ii) Consistent mass matrix. (04 Marks)  
 b. Determine the natural frequencies of stepped bar as shown in Fig.Q.10(b).

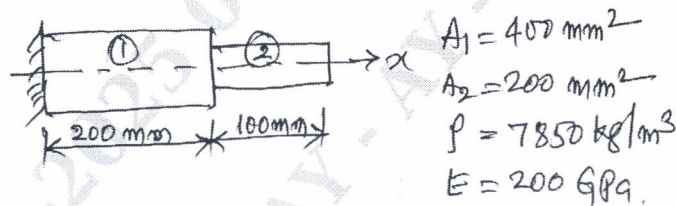


Fig.Q.10(b)

(16 Marks)

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